

Gravitational Corrections (GRS) for RED-SHIFT Observations with the James Webb Space Telescope

Eindhoven University of Technology
The Netherlands
E-mail: HST@quantumlight.science
Website: <https://quantumlight.science>
05/23/2022

Contents:

Example 1: Propagation in the z direction of a Laser – Beam with the speed of light : $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$

Example 2: Propagation of a Beam of Light in the z-direction with the speed of light within a constant gravitational field, oriented in the z-direction, resulting in Gravitational Redshift.

Example 3: Propagation of a Beam of Light in the radial – direction of the [Sun](#) resulting in Gravitational

Redshift (GRS) caused by the : [Gravitational Field of the Sun](#)

Example 4: Deviations in the measured values for the [GRS](#) of the [Sun](#), originating from the

[Gravitational Field of the Sun](#) within the [fusion core](#) of the sun.

Example 5: Propagation of a Beam of Light in the radial – direction of [Sirius](#), resulting in

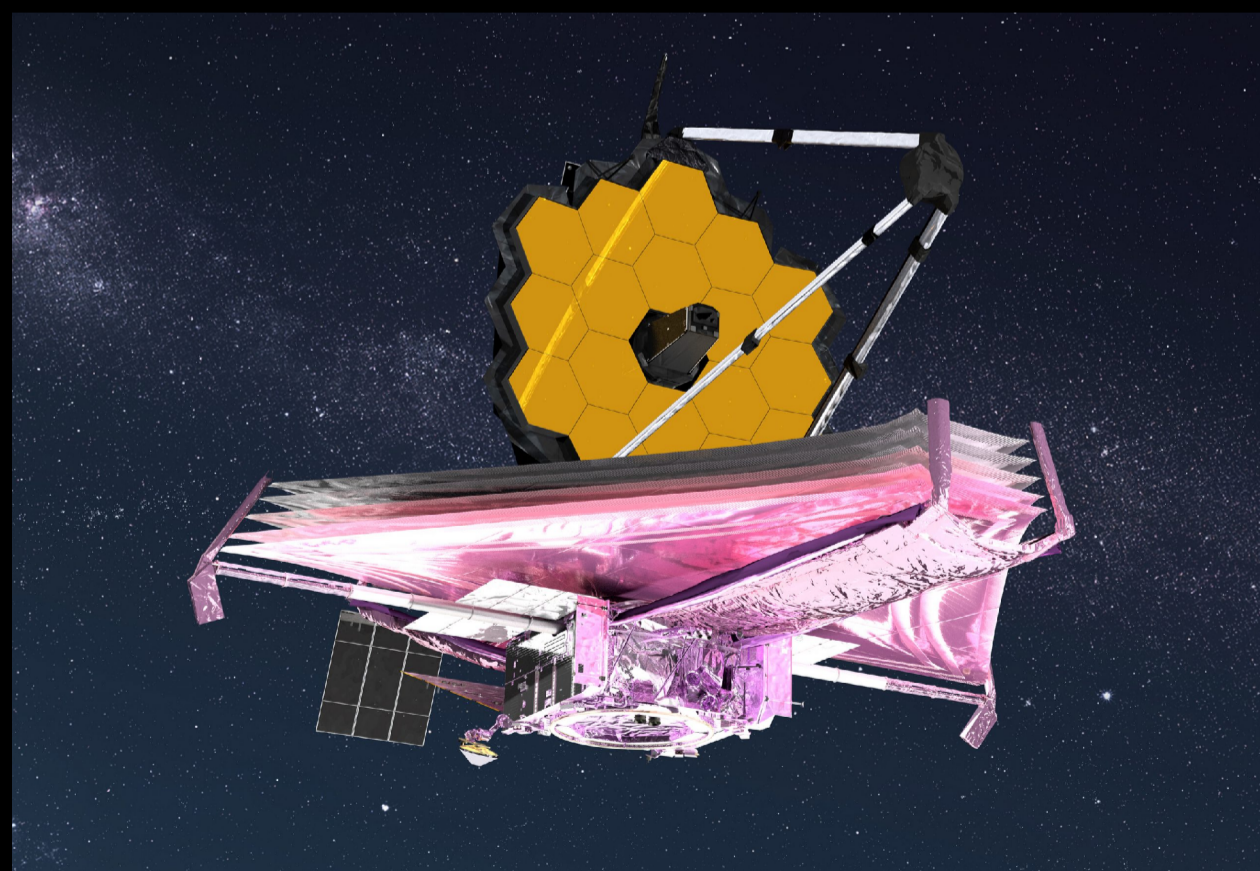
Gravitational Redshift (GRS) caused by the [Gravitational Field of Sirius](#).

Example 6: [The Gravitational Wave Equation.](#) Propagation of a Gravitational Wave in the

z – direction with the speed of light : $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$

Example 7: Spherical Propagation of a Beam of Light in the radial – direction with the speed of light : $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$.

Example 8: Introduction to [Black Holes](#)



All calculations below belong to the book:
[Rising of the James Webb Space Telescope](#)

and its Fundamental Blindness:

All Calculations for Gravitational Intensity Shift and Gravitational RedShift can be downloaded from the [Download Site](https://quantumlight.science/):

<https://quantumlight.science/>

{ev} symbol for [Electric Field Intensity](#) Vector

{mv} symbol for [Magnetic Field Intensity](#) Vector

Run program by : Edit/ Select All/ Shift + Return

Example 1

(Propagation in the z – direction of a Laser –

Beam with the speed of light: $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$)

Book : [Rising of the James Webb Space Telescope and its Fundamental Blindness](#)

Page 15, Equation (19)

$$\begin{aligned}
 & - \frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \\
 & + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}) = 0 \qquad (19)
 \end{aligned}$$

Example of a LASER – BEAM with a Gaussian Intensity division $e^{-K^2 \sqrt{x^2+y^2}}$, combined with an arbitrary division $g[x, y]$ in the (x, y) plane, propagating in the z – direction with the speed of light $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$.

```
In[ ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[ ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:= ε0 = .
```

```
In[• ]:=  $\mu\theta = .$ 
```


```
In[• ]:=  $x = .$ 
```

```
In[• ]:=  $y = .$ 
```

```
In[• ]:=  $z = .$ 
```

```
In[• ]:=  $t = .$ 
```

```
In[• ]:= Get["VectorAnalysis`"]
```

—  **General**: VectorAnalysis` is now obsolete. The legacy version being loaded may conflict wit

```
In[• ]:= InverseFunctions → True
```

```
Out[• ]:= InverseFunctions → True
```

```
In[• ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[• ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[• ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[• ]:= SetCoordinates[Cartesian[x, y, z]]
```

```
Out[• ]:= Cartesian[x, y, z]
```

```
In[• ]:= {Coordinates[Cartesian], CoordinateRanges[Cartesian]}
```

```
Out[• ]:= {{x, y, z}, {-∞ < x < ∞, -∞ < y < ∞, -∞ < z < ∞}}
```

```
In[• ]:= K2 = .
```

$$\text{In}[\bullet] := f[x, y] = g[x, y] e^{-K2 \sqrt{x^2 + y^2}}$$

$$\text{Out}[\bullet] = e^{-K2 \sqrt{x^2 + y^2}} g[x, y]$$

$$\text{In}[\bullet] := \text{ev} = \{f[x, y] * g[t - (K1 / z + 1) * z * \text{Sqrt}[\epsilon\theta] * \text{Sqrt}[\mu\theta]], \theta, \theta\}$$

$$\text{Out}[\bullet] = \left\{ e^{-K2 \sqrt{x^2 + y^2}} g\left[t - \left(1 + \frac{K1}{z}\right) z \sqrt{\epsilon\theta} \sqrt{\mu\theta}\right] \times g[x, y], \theta, \theta \right\}$$

$$\text{In}[\bullet] := \text{mv} = (1 / \text{Sqrt}[\mu\theta]) * \text{Sqrt}[\epsilon\theta] * \{ \theta, f[x, y] * g[t - (K1 / z + 1) * z * \text{Sqrt}[\epsilon\theta] * \text{Sqrt}[\mu\theta]], \theta \}$$

$$\text{Out}[\bullet] = \left\{ \theta, \frac{e^{-K2 \sqrt{x^2 + y^2}} \sqrt{\epsilon\theta} g\left[t - \left(1 + \frac{K1}{z}\right) z \sqrt{\epsilon\theta} \sqrt{\mu\theta}\right] \times g[x, y]}{\sqrt{\mu\theta}}, \theta \right\}$$

Book : [Rising of the James Webb Space Telescope and its Fundament](#)

Example of a LASER – BEAM with a Gaussian Intensity division $e^{-k^2 \sqrt{x^2+y^2}}$ combined with an arbitrary division $g[x, y]$ in the (x, y) plane , propagating i

The input for the Electric Field Intensity $\{E(x, y, z) = ev\}$ and the Magnetic Field Intensity $\{H(x, y, z) = mv\}$ has been substituted in the Field Equation for the Electromagnetic F

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}) = 0 \quad \text{Equation (19)}$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Equation (19) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} = 0$$

In[]:= Div[ev]

$$\text{Out[]}= -\frac{e^{-k^2 \sqrt{x^2+y^2}} k^2 x g\left[t - \left(1 + \frac{k_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \times g[x, y]}{\sqrt{x^2 + y^2}} + e^{-k^2 \sqrt{x^2+y^2}} g\left[t - \left(1 + \frac{k_1}{z}\right) z \sqrt{\epsilon_0}\right]$$

In[•]:= Div[mv]

$$\text{Out}[•] = -\frac{e^{-k_2 \sqrt{x^2+y^2}} k_2 y \sqrt{\epsilon_0} g\left[t - \left(1 + \frac{k_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \times g[x, y]}{\sqrt{x^2+y^2} \sqrt{\mu_0}} + \frac{e^{-k_2 \sqrt{x^2+y^2}} \sqrt{\epsilon_0} g\left[t - \left(1 + \frac{k_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{\sqrt{x^2+y^2} \sqrt{\mu_0}}$$

In[•]:= FullSimplify[%]

$$\text{Out}[•] = \frac{e^{-k_2 \sqrt{x^2+y^2}} \sqrt{\epsilon_0} g\left[t - \left(k_1 + z\right) \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \left(-k_2 y g[x, y] + \sqrt{x^2+y^2} g^{(0,1)}[x, y]\right)}{\sqrt{x^2+y^2} \sqrt{\mu_0}}$$

In[•]:= term1a = D[Cross[ev, mv], t]

$$\text{Out}[•] = \left\{0, 0, \frac{2 e^{-2 k_2 \sqrt{x^2+y^2}} \sqrt{\epsilon_0} g\left[t - \left(1 + \frac{k_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g[x, y]^2 g'\left[t - \left(1 + \frac{k_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{\sqrt{\mu_0}}\right\}$$

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

In[•]:= term1 = ((-ε0) * μ0) * D[Cross[ev, mv], t]

$$\text{Out}[•] = \left\{0, 0, -2 e^{-2 k_2 \sqrt{x^2+y^2}} \epsilon_0^{3/2} \sqrt{\mu_0} g\left[t - \left(1 + \frac{k_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g[x, y]^2 g'\left[t - \left(1 + \frac{k_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]\right\}$$

In[•]:=

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

In[•]:= term2 = ε0 * ev * Div[ev]

$$\text{Out}[•] = \left\{e^{-k_2 \sqrt{x^2+y^2}} \epsilon_0 g\left[t - \left(1 + \frac{k_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \times g[x, y] \left(-\frac{e^{-k_2 \sqrt{x^2+y^2}} k_2 x g\left[t - \left(1 + \frac{k_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{\sqrt{x^2+y^2}}\right.\right.$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

`In[]:= term3 = (-ε0) * Cross[ev, Cur1[ev]]`

$$\text{Out[]} = \left\{ 0, -\epsilon_0 \left(-\frac{e^{-2K_2\sqrt{x^2+y^2}} K_2 y g\left[t - \left(1 + \frac{K_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 g[x, y]^2}{\sqrt{x^2+y^2}} + e^{-2K_2\sqrt{x^2+y^2}} g\left[t - \left(1 + \frac{K_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \right. \right.$$

$$\left. \left. e^{-2K_2\sqrt{x^2+y^2}} \epsilon_0^{3/2} \sqrt{\mu_0} g\left[t - \left(1 + \frac{K_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g[x, y]^2 g'\left[t - \left(1 + \frac{K_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \right. \right.$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

`In[]:= term4 = μ0 * mv * Div[mv]`

$$\text{Out[]} = \left\{ 0, e^{-K_2\sqrt{x^2+y^2}} \sqrt{\epsilon_0} \sqrt{\mu_0} g\left[t - \left(1 + \frac{K_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \times g[x, y] \left(-\frac{e^{-K_2\sqrt{x^2+y^2}} K_2 y \sqrt{\epsilon_0} g}{\sqrt{x^2+y^2}} \right. \right.$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

`In[]:= term5 = (-μ0) * Cross[mv, Cur1[mv]]`

$$\text{Out[]} = \left\{ -\mu_0 \left(-\frac{e^{-2K_2\sqrt{x^2+y^2}} K_2 x \epsilon_0 g\left[t - \left(1 + \frac{K_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 g[x, y]^2}{\sqrt{x^2+y^2} \mu_0} + \frac{e^{-2K_2\sqrt{x^2+y^2}} \epsilon_0 g\left[t - \left(1 + \frac{K_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{\mu_0} \right. \right.$$

$$\left. \left. 0, e^{-2K_2\sqrt{x^2+y^2}} \epsilon_0^{3/2} \sqrt{\mu_0} g\left[t - \left(1 + \frac{K_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g[x, y]^2 g'\left[t - \left(1 + \frac{K_1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \right. \right.$$

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}) = 0 : \text{Book Page}$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Equation (19) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} = 0$$

`In[]:=` `vergelijking = term1 + term2 + term3 + term4 + term5`

$$\text{Out[]} = \left\{ e^{-k_2 \sqrt{x^2+y^2}} \epsilon_0 g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right] \times g[x, y] \left(-\frac{e^{-k_2 \sqrt{x^2+y^2}} k_2 x g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]}{\sqrt{x^2+y^2}} \right. \right.$$

$$\left. \mu_0 \left(-\frac{e^{-2k_2 \sqrt{x^2+y^2}} k_2 x \epsilon_0 g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 g[x, y]^2}{\sqrt{x^2+y^2} \mu_0} + \frac{e^{-2k_2 \sqrt{x^2+y^2}} \epsilon_0 g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]}{\sqrt{x^2+y^2}} \right) \right.$$

$$\left. e^{-k_2 \sqrt{x^2+y^2}} \sqrt{\epsilon_0} \sqrt{\mu_0} g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right] \times g[x, y] \left(-\frac{e^{-k_2 \sqrt{x^2+y^2}} k_2 y \sqrt{\epsilon_0} g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]}{\sqrt{x^2+y^2}} \right) \right.$$

$$\left. \epsilon_0 \left(-\frac{e^{-2k_2 \sqrt{x^2+y^2}} k_2 y g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 g[x, y]^2}{\sqrt{x^2+y^2}} + e^{-2k_2 \sqrt{x^2+y^2}} g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right] \right) \right\}$$

`In[]:=`

The electromagnetic force density in the x - direction equals :

`In[•]:= xvergelijking = term1[[1]] + term2[[1]] + term3[[1]] + term4[[1]] + term5[[1]]`

$$\text{Out[•]} = e^{-k_2 \sqrt{x^2+y^2}} \epsilon_0 g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right] \times g[x, y] \left(- \frac{e^{-k_2 \sqrt{x^2+y^2}} k_2 x g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]}{\sqrt{x^2+y^2}} \right. \\ \left. \mu_0 \left(- \frac{e^{-2 k_2 \sqrt{x^2+y^2}} k_2 x \epsilon_0 g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 g[x, y]^2}{\sqrt{x^2+y^2} \mu_0} + \frac{e^{-2 k_2 \sqrt{x^2+y^2}} \epsilon_0 g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]}{\sqrt{x^2+y^2}} \right) \right)$$

`In[•]:= FullSimplify[%]`

`Out[•]= 0`

`In[•]:= xvergelijking1 = %`

`Out[•]= 0`

The electromagnetic force density in the y - direction equals:

`In[•]:= yvergelijking = term1[[2]] + term2[[2]] + term3[[2]] + term4[[2]] + term5[[2]]`

$$\text{Out[•]} = e^{-k_2 \sqrt{x^2+y^2}} \sqrt{\epsilon_0} \sqrt{\mu_0} g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right] \times g[x, y] \left(- \frac{e^{-k_2 \sqrt{x^2+y^2}} k_2 y \sqrt{\epsilon_0} g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]}{\sqrt{x^2+y^2}} \right. \\ \left. \epsilon_0 \left(- \frac{e^{-2 k_2 \sqrt{x^2+y^2}} k_2 y g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 g[x, y]^2}{\sqrt{x^2+y^2}} + e^{-2 k_2 \sqrt{x^2+y^2}} g \left[t - \left(1 + \frac{k_1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right] \right) \right)$$

`In[•]:= FullSimplify[%]`

`Out[•]= 0`

`In[•]:= yvergelijking1 = %`

`Out[•]= 0`

The electromagnetic force density in the z - direction equals :

```
In[ ]:= zvergelijking = term1[[3]] + term2[[3]] + term3[[3]] + term4[[3]] +
term5[[3]]
```

```
Out[ ]:= 0
```

```
In[ ]:= FullSimplify[%]
```

```
Out[ ]:= 0
```

```
In[ ]:= zvergelijking1 = %
```

```
Out[ ]:= 0
```

Results for the electromagnetic force densities in resp x-direction, y-direction, z-direction:

```
In[ ]:= xvergelijking1
```

```
Out[ ]:= 0
```

```
In[ ]:= yvergelijking1
```

```
Out[ ]:= 0
```

```
In[ ]:= zvergelijking1
```

```
Out[ ]:= 0
```

According the force-density equations in the x-direction, y-direction and z-direction, the solution is zero in every direction. This **Perfect Equilibrium** does **only** exist when the Electric field represents the solution for [equation \(19\) on page 16](#).

Example 2

Propagation of a Beam of Light in the z-direction with the speed of light: $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$ within a constant gravitational field, oriented in the z-direction. **Gravitational Redshift.**

```
In[ ]:=
```

Book : [Rising of the James Webb Space Telescope and its Fundamentals](#)

Example of a Spherical Beam of Light , propagating in the radial – direction

with the speed of light $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$.

The input for the Electric Field Intensity $\{E(x, y, z, t) = ev\}$ and the Magnetic Field Intensity $\{H(x, y, z, t) = hv\}$ into the Poynting Vector Equation for the Electromagnetic Field within a constant gravitational field with a metric tensor $g_{\mu\nu}$.

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}) + \frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) g$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) g$$

Equation (73) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} + \text{term6} = 0$$

In[]:= $\epsilon_0 =$.

In[]:= $\mu_0 =$.

```
In[ ]:= x =.
```

```
In[ ]:= y =.
```

```
In[ ]:= z =.
```

```
In[ ]:= t =.
```

```
In[ ]:= Get["VectorAnalysis`"]
```

— **General**: VectorAnalysis` is now obsolete. The legacy version being loaded may conflict with

```
In[ ]:= Get["Calculus`DSolve`"]
```

— **Get**: Cannot open Calculus`DSolve`.

```
Out[ ]:= $Failed
```

```
In[ ]:= InverseFunctions → True
```

```
Out[ ]:= InverseFunctions → True
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[ ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:= Get["Calculus`DSolveIntegrals`"]
```

— **Get**: Cannot open Calculus`DSolveIntegrals`.

```
Out[ ]:= $Failed
```

`In[•]:= SetCoordinates[Cartesian[x, y, z]]`

`Out[•]= Cartesian[x, y, z]`

`In[•]:= {Coordinates[Cartesian], CoordinateRanges[Cartesian]}`

`Out[•]= {{x, y, z}, {-∞ < x < ∞, -∞ < y < ∞, -∞ < z < ∞}}`

`In[•]:= G1 = .`

`In[•]:= ev = {e-1/2 G1 z ε0 μ0 g[e-G1 ε0 μ0 (t - z √ε0 √μ0)], 0, 0}`

`Out[•]= {e-1/2 G1 z ε0 μ0 g[e-G1 ε0 μ0 (t - z √ε0 √μ0)], 0, 0}`

`In[•]:= mv = (1/Sqrt[μ0])*Sqrt[ε0]*
{0, e-1/2 G1 z ε0 μ0 g[e-G1 ε0 μ0 (t - z √ε0 √μ0)], 0}`

`Out[•]= {0, $\frac{e^{-\frac{1}{2} G1 z \epsilon_0 \mu_0} \sqrt{\epsilon_0} g[e^{-G1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})]}{\sqrt{\mu_0}}$, 0}`

`In[•]:= gv = {0, 0, G1}`

`Out[•]= {0, 0, G1}`

`In[•]:= Intensity = - $\frac{1}{2}$ (ε0 (Dot[ev, ev]) + μ0 (Dot[mv, mv]))`

`Out[•]= - $\frac{1 (e^{-G1 z \epsilon_0 \mu_0} \epsilon_0 g[e^{-G1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})]^2 + e^{-G1 z \epsilon_0 \mu_0} g[e^{-G1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})])}{2}$`

`In[•]:= FullSimplify[%]`

`Out[•]= - $\frac{e^{-G1 z \epsilon_0 \mu_0} g[e^{-G1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})]^2 1 (\epsilon_0 + \epsilon_0)}{2}$`

In[•]:= Div[ev]

Out[•]= 0

In[•]:= Div[mv]

Out[•]= 0

In[•]:= FullSimplify[%]

Out[•]= 0

In[•]:= term1a = D[Cross[ev, mv], t]

Out[•]= {0, 0, $\frac{2 e^{-G1 \epsilon_0 \mu_0 - G1 z \epsilon_0 \mu_0} \sqrt{\epsilon_0} g[e^{-G1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})] g'[e^{-G1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})]}{\sqrt{\mu_0}}$ }

In[•]:=

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}.$$

In[•]:= term1 = ((-ε0)*μ0)*D[Cross[ev, mv], t]

Out[•]= {0, 0, $-2 e^{-G1 \epsilon_0 \mu_0 - G1 z \epsilon_0 \mu_0} \epsilon_0^{3/2} \sqrt{\mu_0} g[e^{-G1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})] g'[e^{-G1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})]$ }

In[•]:=

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}).$$

In[•]:= term2 = ε0*ev*Div[ev]

Out[•]= {0, 0, 0}

In[•]:=

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}).$$

In[]:= term3 = (-ε0)*Cross[ev, Curl[ev]]

Out[]:= {0, 0, -ε0 (-1/2 e^{-G1 z ε0 μ0} G1 ε0 μ0 g [e^{-G1 ε0 μ0} (t - z √ε0 √μ0)]^2 - e^{-G1 ε0 μ0 - G1 z ε0 μ0} √ε0 √μ0}

In[]:=

term4 = μ0 H (∇ . H) .

In[]:= term4 = μ0 * mv * Div[mv]

Out[]:= {0, 0, 0}

In[]:=

term5 = -μ0 H × (∇ × H) .

In[]:= term5 = (-μ0)*Cross[mv, Curl[mv]]

Out[]:= {0, 0, -μ0 (-1/2 e^{-G1 z ε0 μ0} G1 ε0^2 g [e^{-G1 ε0 μ0} (t - z √ε0 √μ0)]^2 - e^{-G1 ε0 μ0 - G1 z ε0 μ0} ε0^{3/2}}

term6 = -1/2 (ε^2 μ (E . E) + ε μ^2 (H . H)) g

In[]:= term6 = - ((ε0^2 μ0 / 2) Dot[ev, ev] + (ε0 μ0^2 / 2) Dot[mv, mv]) gv

Out[]:= {0, 0, -e^{-G1 z ε0 μ0} G1 ε0^2 μ0 g [e^{-G1 ε0 μ0} (t - z √ε0 √μ0)]^2}

In[]:= vergelijking = term1 + term2 + term3 + term4 + term5 + term6

Out[]:= {0, 0, -e^{-G1 z ε0 μ0} G1 ε0^2 μ0 g [e^{-G1 ε0 μ0} (t - z √ε0 √μ0)]^2 - 2 e^{-G1 ε0 μ0 - G1 z ε0 μ0} ε0^{3/2} √μ0
μ0 (-1/2 e^{-G1 z ε0 μ0} G1 ε0^2 g [e^{-G1 ε0 μ0} (t - z √ε0 √μ0)]^2 - e^{-G1 ε0 μ0 - G1 z ε0 μ0} ε0^{3/2} g [e^{-G1
ε0 (-1/2 e^{-G1 z ε0 μ0} G1 ε0 μ0 g [e^{-G1 ε0 μ0} (t - z √ε0 √μ0)]^2 - e^{-G1 ε0 μ0 - G1 z ε0 μ0} √ε0 √μ0

In[]:=

The electromagnetic force density in the x - direction equals :

`In[•]:= xvergelijking = term1[1] + term2[1] + term3[1] + term4[1] + term5[1] + term6[1]`

`Out[•]= 0`

`In[•]:= FullSimplify[%]`

`Out[•]= 0`

`In[•]:= xvergelijking1 = %`

`Out[•]= 0`

`In[•]:=`

The electromagnetic force density in the y - direction equals :

`In[•]:= yvergelijking = term1[2] + term2[2] + term3[2] + term4[2] + term5[2] + term6[2]`

`Out[•]= 0`

`In[•]:= FullSimplify[%]`

`Out[•]= 0`

`In[•]:= yvergelijking1 = %`

`Out[•]= 0`

`In[•]:=`

The electromagnetic force density in the z - direction equals :

`In[•]:= zvergelijking = term1[3] + term2[3] + term3[3] + term4[3] + term5[3] + term6[3]`

`Out[•]=`

$$-e^{-G_1 z \epsilon_0 \mu_0} G_1 \epsilon_0^2 \mu_0 g \left[e^{-G_1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0}) \right]^2 - 2 e^{-G_1 \epsilon_0 \mu_0 - G_1 z \epsilon_0 \mu_0} \epsilon_0^{3/2} \sqrt{\mu_0} g \left[e^{-G_1 \epsilon_0 \mu_0 - G_1 z \epsilon_0 \mu_0} \epsilon_0^{3/2} g \left[e^{-G_1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0}) \right]^2 - \frac{e^{-G_1 \epsilon_0 \mu_0 - G_1 z \epsilon_0 \mu_0} \epsilon_0^{3/2} g \left[e^{-G_1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0}) \right]^2}{\epsilon_0} \right]$$

$$\epsilon_0 \left(-\frac{1}{2} e^{-G_1 z \epsilon_0 \mu_0} G_1 \epsilon_0 \mu_0 g \left[e^{-G_1 \epsilon_0 \mu_0} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0}) \right]^2 - e^{-G_1 \epsilon_0 \mu_0 - G_1 z \epsilon_0 \mu_0} \sqrt{\epsilon_0} \sqrt{\mu_0} g \right)$$

In[•]:= FullSimplify[%]

Out[•]= 0

In[•]:= zvergelijking1 = %

Out[•]= 0

Results force densities in resp x-direction, y-direction, z-direction

Results for the ~~electromagnetic~~ force densities in resp x-direction, y-direction, z-direction:

In[•]:= xvergelijking1

Out[•]= 0

In[•]:= yvergelijking1

Out[•]= 0

In[•]:= zvergelijking1

Out[•]= 0

According the force-density equations in the x-direction, y- equals zero in every direction. This represents the solution for e . It follows from the mathematical solution for the electromagnetic $ev = e^{-\frac{1}{2} G1 z \epsilon0 \mu0} g \left[e^{-G1 \epsilon0 \mu0} (t - z \sqrt{\epsilon0} \sqrt{\mu0}) \right]$

that the **intensity increases** with the value:

$$\text{Intensity} = -\frac{1}{2} (\epsilon0 (\text{Dot}[ev, ev]) + \mu0 (\text{Dot}[mv, mv]))$$

$$= \frac{1}{2} \left(e^{-\frac{G1 z \epsilon0 \mu0}{2}} \epsilon0 g \left[e^{-G1 \epsilon0 \mu0} (t - z \sqrt{\epsilon0} \sqrt{\mu0}) \right]^2 + e^{-\frac{G1 z \epsilon0 \mu0}{2}} g \left[e^{-G1 \epsilon0 \mu0} (t - z \sqrt{\epsilon0} \sqrt{\mu0}) \right]^2 \epsilon0 \right)$$

The Electromagnetic Energy ~~Intensity~~ is proportional to: $e^{-G1 z \epsilon0 \mu0}$ distance z in the direction **opposite** to the z -direction of the gravitational energy. The frequency is proportional to the energy density (book: Equation energy). The speed of light remains **constant** in a gravitational field.

Within a Constant Gravitational Field G_1 The observed Cosmo

$$\omega_{\text{NLGR}} = \omega_0 e^{-g z \mu_0 \epsilon_0} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

The term $\left(\frac{\Delta \omega}{\omega} = e^{-g z \mu_0 \epsilon_0}\right)$

in Quantum Light Theory (QLT) differs

from the second term $\frac{1}{2!} \left(-g z \mu_0 \epsilon_0\right)^2$ in Taylors Series of the exp

the Classical Gravitational Frequency Shift:

$\left(\frac{\Delta \omega}{\omega} = -g z \mu_0 \epsilon_0\right)$ in General Relativity presented in

An improved approach for testing Gravitational Redshift via
Satellite-Base three frequency links combination

Example 3

Propagation of a Beam of Light in the radial-direction
of the Sun from the Gravitational Radius of the sun until
with the speed of light $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$

within a Radial Gravitational Field G_1 oriented in the r
resulting in Gravitational Redshift $\nu_{\text{Grav-1}}$ (GRS) caused

There are two kinds of Redshift caused by the gravitational field of the

1) Redshift₁ caused by the Gravitational Field within the fusion core
(created). This has been calculated in Example 3

2) Redshift₂ caused by the Gravitational Field outside the fusion core

The total RedShift caused by the Gravitational Field of the sun is the s

Book : [Rising of the James Webb Space Telescope and its Fundamental Bli](#)

Example of a Spherical Beam of Light , propagating in the radial – direction

with the speed of light $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$.

The input for the Electric Field Intensity $(E(x, y, z) = e_x)$ and the Magnetic Field

The input for the Electric Field Intensity $\{\vec{E}(x, y, z, t) = -\nabla V\}$ and the Magnetic Field \vec{H} for the Electromagnetic Field within a constant gravitational field with acceleration g is:

$$-\frac{1}{c^2} \frac{\partial(\vec{E} \times \vec{H})}{\partial t} + \epsilon_0 \vec{E} (\nabla \cdot \vec{E}) - \epsilon_0 \vec{E} \times (\nabla \times \vec{E}) + \mu_0 \vec{H} (\nabla \cdot \vec{H}) - \mu_0 \vec{H} \times (\nabla \times \vec{H}) + \frac{1}{2} \left(\epsilon^2 \mu \left(\vec{E} \cdot \vec{E} \right) + \epsilon \mu^2 \left(\vec{H} \cdot \vec{H} \right) \right) g$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\vec{E} \times \vec{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \vec{E} (\nabla \cdot \vec{E})$$

$$\text{term3} = -\epsilon_0 \vec{E} \times (\nabla \times \vec{E})$$

$$\text{term4} = \mu_0 \vec{H} (\nabla \cdot \vec{H})$$

$$\text{term5} = -\mu_0 \vec{H} \times (\nabla \times \vec{H})$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\vec{E} \cdot \vec{E} \right) + \epsilon \mu^2 \left(\vec{H} \cdot \vec{H} \right) \right) g$$

Equation (73) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} + \text{term6} = 0$$

In[]:= $\epsilon_0 =$

```
In[ ]:=  $\mu_0 =.$ 
```

```
In[ ]:= x =.
```

```
In[ ]:= y =.
```

```
In[ ]:= z =.
```

```
In[ ]:= t =.
```

```
In[ ]:= Get["VectorAnalysis`"]
```

— **General**: VectorAnalysis` is now obsolete. The legacy version being loaded may conflict with

```
In[ ]:= Get["Calculus`DSolve`"]
```

— **Get**: Cannot open Calculus`DSolve`.

```
Out[ ]:= $Failed
```

```
In[ ]:= InverseFunctions → True
```

```
Out[ ]:= InverseFunctions → True
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[ ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:= Get["Calculus`DSolveIntegrals`"]
```

— **Get**: Cannot open Calculus`DSolveIntegrals`.

```
Out[ ]:= $Failed
```

```
In[• ]:= SetCoordinates[Cartesian[x, y, z]]
```

```
Out[• ]:= Cartesian[x, y, z]
```

```
In[• ]:= G1 = .
```

```
In[• ]:=  $\epsilon_0$  = .
```

```
In[• ]:=  $\mu_0$  = .
```

```
In[• ]:= fg = .
```

```
In[• ]:= Msun = .
```

The light being emitted by the sun has been created by **nuclear fusion in the core**

Outside the **Gravitational Radius** of the Sun, (the distance of the center of the sun where the generated light will propagate with the speed of light :

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$

oppositely directed towards the gravitational acceleration outside the sun. The gravitational acceleration outside the sun will increase proportionally

$$g^2[r] = K_2 \frac{1}{r^2} = \frac{f_g M_{\text{Sun}}}{4\pi} \frac{1}{r^2}$$

within a **Radial Gravitational Field** $g[r]$ oriented

in the radial – direction of the **Sun** with **acceleration** $g[r]$ resulting in the

Gravitational Redshift caused by the **Gravitational Field outside the Sun**.

The **Gravitational Intensity Shift** for the light emitted by the sun equals

$$I_{\text{NGR}} = e^{-\frac{K_2 \epsilon_0 \mu_0}{z}}$$

Instead of Spherical Coordinates (r, θ, φ) for the light emitted Spherically

for the far field (within a small area like the dimensions of a **Space Telescope**)

Cartesian Coordinates (x, y, z) are being used.

$$\text{In}[\bullet] := \epsilon_0 = .$$

$$\text{In}[\bullet] := \mu_0 = .$$

$$\text{In}[\bullet] := f_g = .$$

`In[•]:= Msun = .`

`In[•]:= K1 = .`

`In[•]:= K2 = .`

`In[•]:= h[z] = K3 e- $\frac{K2 \epsilon_0 \mu_0}{2z}$ }`

`Out[•]:= e- $\frac{K2 \epsilon_0 \mu_0}{2z}$ } K3`

`In[•]:= ev = {h[z] × g[t - z √ ϵ_0 √ μ_0], 0, 0}`

`Out[•]:= {e- $\frac{K2 \epsilon_0 \mu_0}{2z}$ } K3 g[t - z √ ϵ_0 √ μ_0], 0, 0}`

`In[•]:= mv = (1/Sqrt[μ_0]) * Sqrt[ϵ_0] *
{0, h[z] × g[t - z √ ϵ_0 √ μ_0], 0}`

`Out[•]:= {0, $\frac{e^{-\frac{K2 \epsilon_0 \mu_0}{2z}} K3 \sqrt{\epsilon_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}}$, 0}`

`In[•]:= g2 = {0, 0, $-\frac{K2}{z^2}$ }`

`Out[•]:= {0, 0, $-\frac{K2}{z^2}$ }`

`In[•]:= Intensity = $\frac{1}{2}$ (ϵ_0 (Dot[ev, ev]) + μ_0 (Dot[mv, mv]))`

`Out[•]:= $\frac{1}{2} \left(e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 \epsilon_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 + e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 \epsilon_0 \right)$`

2

In[]:= FullSimplify[%]

$$\text{Out[]} = \frac{e^{-\frac{k^2 \epsilon_0 \mu_0}{z}} k^3 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 \mathbf{1} (\epsilon_0 + \epsilon_0)}{2}$$

In[]:= Div[ev]

$$\text{Out[]} = 0$$

In[]:= Div[mv]

$$\text{Out[]} = 0$$

In[]:= FullSimplify[%]

$$\text{Out[]} = 0$$

In[]:= term1a = D[Cross[ev, mv], t]

$$\text{Out[]} = \left\{ 0, 0, \frac{2 e^{-\frac{k^2 \epsilon_0 \mu_0}{z}} k^3 \sqrt{\epsilon_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}} \right\}$$

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

In[]:= term1 = ((-epsilon0)*mu0)*D[Cross[ev, mv], t]

$$\text{Out[]} = \left\{ 0, 0, -2 e^{-\frac{k^2 \epsilon_0 \mu_0}{z}} k^3 \epsilon_0^{3/2} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right\}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

In[]:= term2 = epsilon0*ev*Div[ev]

$$\text{Out[]} = \{0, 0, 0\}$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

In[]:= term3 = (-ε0)*Cross[ev, Curl[ev]]

$$\text{Out[]} = \left\{ 0, 0, -\epsilon_0 \left(\frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_3^2 \sqrt{\epsilon_0} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right) \right\}$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

In[]:= term4 = μ0 * mv * Div[mv]

$$\text{Out[]} = \{0, 0, 0\}$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

In[]:= term5 = (-μ0)*Cross[mv, Curl[mv]]

$$\text{Out[]} = \left\{ 0, 0, -\mu_0 \left(\frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0^2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - \frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_3^2 \epsilon_0^{3/2} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}} \right) \right\}$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\overline{\mathbf{E} \cdot \mathbf{E}} \right) + \epsilon \mu^2 \left(\overline{\mathbf{H} \cdot \mathbf{H}} \right) \right) g$$

In[]:= term6 = -\left(\frac{\epsilon_0^2 \mu_0}{2} \text{Dot}[ev, ev] + \frac{\epsilon_0 \mu_0^2}{2} \text{Dot}[mv, mv] \right) g^2

$$\text{Out[]} = \left\{ 0, 0, \frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0^2 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{z^2} \right\}$$

In[]:= vergelijking = term1 + term2 + term3 + term4 + term5 + term6

$$\text{Out[]} = \left\{ 0, 0, \frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0^2 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{z^2} - 2 e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_3^2 \epsilon_0^{3/2} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right. \\ \left. \mu_0 \left(\frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0^2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - \frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_3^2 \epsilon_0^{3/2} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}} \right) \right. \\ \left. \epsilon_0 \left(\frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_3^2 \sqrt{\epsilon_0} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right) \right\}$$

In[•]:=

The electromagnetic force density in the x - direction equals :

In[•]:= xvergelijking = term1[1] + term2[1] + term3[1] + term4[1] +
term5[1] + term6[1]

Out[•]= 0

In[•]:= FullSimplify[%]

Out[•]= 0

In[•]:= xvergelijking1 = %

Out[•]= 0

In[•]:=

The electromagnetic force density in the y - direction equals :

In[•]:= yvergelijking = term1[2] + term2[2] + term3[2] + term4[2] +
term5[2] + term6[2]

Out[•]= 0

In[•]:= FullSimplify[%]

Out[•]= 0

In[•]:= yvergelijking1 = %

Out[•]= 0

The electromagnetic force density in the z - direction equals :

In[]:= zvergelijking = term1[3] + term2[3] + term3[3] + term4[3] +
term5[3] + term6[3]

$$\text{Out[]} = \frac{e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K2 K3^2 \epsilon_0^2 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{z^2} - 2 e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 \epsilon_0^{3/2} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \epsilon_0$$

$$\mu_0 \left(\frac{e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K2 K3^2 \epsilon_0^2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - \frac{e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 \epsilon_0^{3/2} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}} \right)$$

$$\epsilon_0 \left(\frac{e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K2 K3^2 \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 \sqrt{\epsilon_0} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right)$$

In[]:= FullSimplify[%]

Out[]= 0

In[]:= zvergelijking1 = %

Out[]= 0

Results for the electromagnetic force densities in resp x-direction, y-direction, z-direction:

In[]:= xvergelijking1

Out[]= 0

In[]:= yvergelijking1

Out[]= 0

In[]:= zvergelijking1

Out[]= 0

According the force-density equations in the x-direction, y-direction and z-direction, the electromagnetic force density is zero in every direction. This represents the solution for equation (73) on page 27. It follows from the mathematical solution for the electromagnetic field

$$E_v = e^{-\frac{K2 \epsilon_0 \mu_0}{z}} g \left[e^{-\frac{K2 \epsilon_0 \mu_0}{2z}} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0}) \right]$$

that the **intensity increases** with the value:

$$\text{Intensity} = \frac{1}{2} (\epsilon_0 (\text{Dot}[ev, ev]) + \mu_0 (\text{Dot}[mv, mv])) =$$

$$= e^{-\frac{K2 \epsilon_0 \mu_0}{z}} \epsilon_0 g \left[e^{-\frac{K2 \epsilon_0 \mu_0}{2z}} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0}) \right]^2$$

The Electromagnetic Energy Intensity is proportional to: $e^{-\frac{K2 \epsilon_0 \mu_0}{z}}$ along distance z in the direction **opposite** to the z -direction of the gravitation

The frequency is proportional to the energy density ([book: Equation 98 Page](#))

The speed of light remains **constant** in a gravitational field.

Within a Gravitational Field $\frac{K2}{z^2}$ The observed Cosmological Redshift

$$\omega_{\text{NLGR}} = \omega_0 e^{-\frac{K2 \epsilon_0 \mu_0}{z}} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

$$\text{The term } \left(\frac{\Delta \omega}{\omega} = e^{-\frac{K2 \epsilon_0 \mu_0}{z}} \right)$$

has been presented in generally as a **GRS** Redshift comparable with the generated by a velocity v_{Doppler} :

$$v_{\text{Doppler}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{K2 \epsilon_0 \mu_0}{z}}$$

There are two types of **GRS** generated by the sun.

1) GRS generated inside the sun where the gravitational field is proportional

$g[z] = K1 z$ with the Solution:

$$v_{\text{Doppler-1}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{1}{4} K1 z^2 \mu_0 \epsilon_0}$$

([book, page 64, Equation \(111\)](#))

2) GRS generated outside the sun where the gravitational field is proportional to the radial distance $\frac{1}{z^2}$

$g[z] = K2 \frac{1}{z^2}$ with the Solution:

$$v_{\text{Doppler-2}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{K2 \epsilon_0 \mu_0}{z}}$$

(book, page 64, Equation (111))

$$\text{In}[] := \text{Intensity} = -\frac{1}{2} (\epsilon_0 (\text{Dot}[\text{ev}, \text{ev}]) + \mu_0 (\text{Dot}[\text{mv}, \text{mv}]))$$

$$\text{Out}[] = -\frac{1 \left(e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 \epsilon_0 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 + e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 \epsilon_0 \right)}{2}$$

$$\text{In}[] := \text{FullSimplify}[\%]$$

$$\text{Out}[] = -\frac{e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 1 (\epsilon_0 + \epsilon_0)}{2}$$

2) GRS generated outside the sun where the gravitational field to the radial distance $\frac{1}{z^2}$

$g[z] = K2 \frac{1}{z^2}$ with the Solution:

$$v_{\text{Doppler-2}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{K2 \epsilon_0 \mu_0}{z}}$$

(book, page 64, Equation (111))

$$v_{\text{Doppler-1}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{K2 \epsilon_0 \mu_0}{z_2}} - c e^{-\frac{K2 \epsilon_0 \mu_0}{z_1}}$$

With:

$z_1 =$ Radius of the sun

$z_2 =$ Distance between the sun and the Earth

$$\text{In}[] := c = 3 \times 10^8$$

$$\text{Out}[] = 300000000$$

```
In[ ]:= ε0 = 8.85 × 10-12
```

```
Out[ ]= 8.85 × 10-12
```

```
In[ ]:= μ0 = 4 π 10-7
```

```
Out[ ]=  $\frac{\pi}{2500000}$ 
```

```
In[ ]:= fg = 6.67428 × 10-11
```

```
Out[ ]= 6.67428 × 10-11
```

```
In[ ]:= K2 =  $\frac{fg \text{ Msun}}{4 \pi}$ 
```

```
Out[ ]= 1.05612 × 1019
```

```
Msun = 1.98892 1030
```

```
Out[ ]= 1.98847 × 1030
```

```
In[ ]:= RSun = 69 634 000
```

```
Out[ ]= 69 634 000
```

The energy from the Sun, both heat and light energy, originates from a nuclear fusion process that is occurring inside the core. The type of fusion that occurs inside of the Sun is known as proton – proton fusion.

Inside the Sun, this process begins with protons (which is simply a hydrogen atom). As these protons fuse together and are turned into helium. This fusion process and the transformation results in a release of energy that keeps the sun shining and moves across the solar system. It is important to note that the core is the only place where fusion of heat through fusion (it contributes about 99 × %). The rest of the Sun's energy is transported

The sun looks like a featureless yellow orb from Earth, but it has discrete internal layers. The central core, which is the only place where fusion happens, extends to a radius of 138 000 kilometers. Beyond that, the rest of the sun is made up of

and the convective zone reaches to the photosphere. At a radius of 695 000 kilometers the photosphere is the deepest layer that astronomers can observe directly and is the closest the sun has to a surface. The most intense part of the emission spectrum of the sun takes place at about 1 / 3 of the the radius (138 000 kilometers) of the sun.

$$z1 = 55\,000\,000$$

This is the area where the emitted spectra of the sun has been detected by astronomers.

Out[]:=
69634000

In[]:= z1 = 55 000 000

Out[]:= 55 000 000

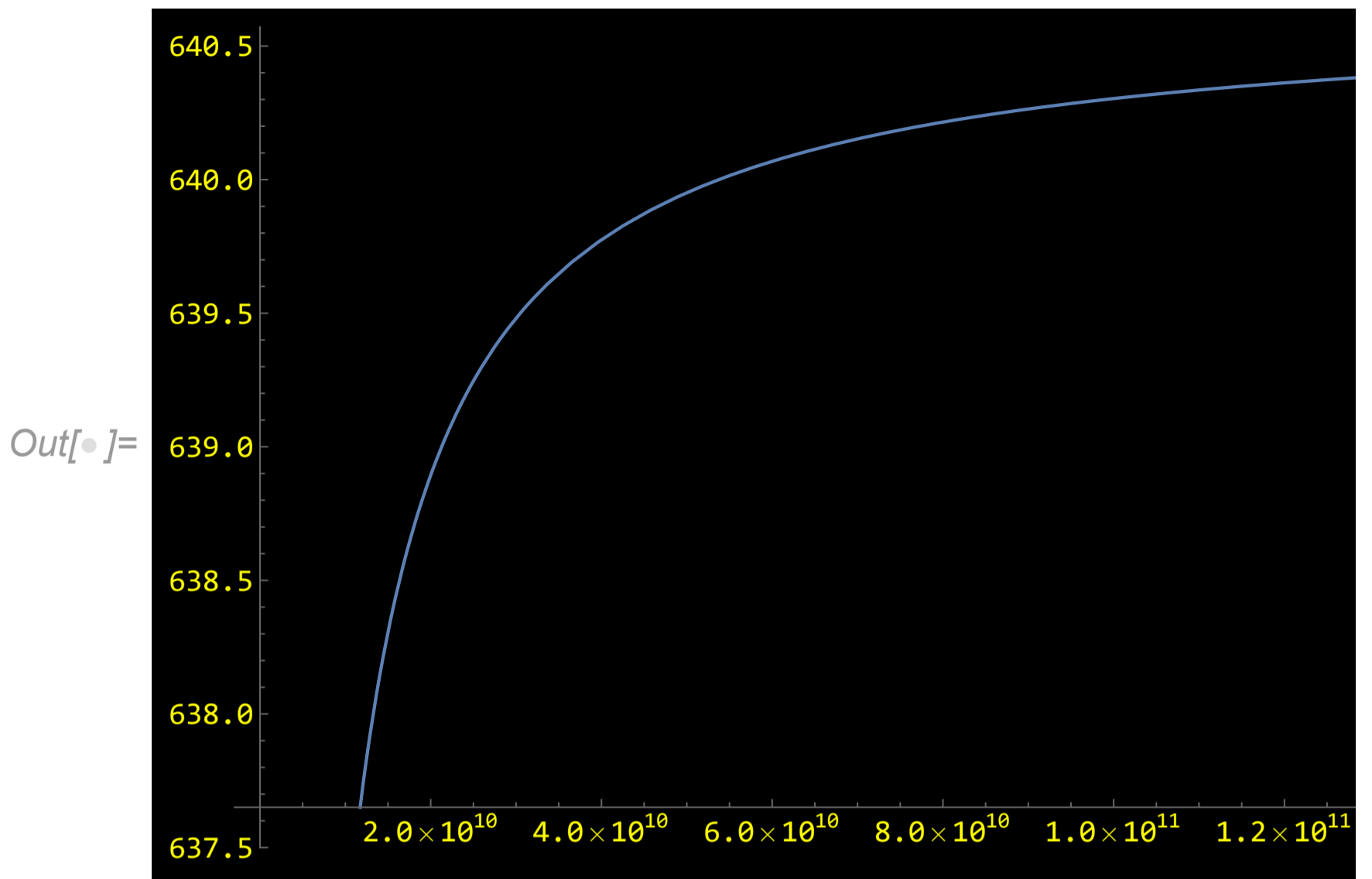
The distance between Sun and Earth equals z2

In[]:= z2 = 149 597 870 700

Out[]:= 149 597 870 700

The Gravitational Doppler Shift from the emitting area of the fusion core of the sun is presented below :

In[]:= $\text{Plot}\left[c \left(e^{-\frac{K2 \epsilon_0 \mu_0}{z}} - e^{-\frac{K2 \epsilon_0 \mu_0}{z1}} \right), \{z, z1, z2\}\right]$



$$v_{\text{Doppler}} = c \left(e^{-\frac{K2 \epsilon_0 \mu_0}{z2}} - e^{-\frac{K2 \epsilon_0 \mu_0}{z1}} \right)$$

Out[]:= 640.42

In[]:=

The calculated value of 640.4 [m/s] for the GRS of the Sun corresponds to the measured average value for the GRS of the Sun published in :

The solar gravitational redshift from HARPS – LFC
Moon spectra. (A test of the general theory of relativity)

Example 4

Deviations in the measured values for the GRS of the Sun originating from the Gravitational Field of the Sun with

Book : [Rising of the James Webb Space Telescope and its Fundamental Blurred](#)

Example of a Spherical Beam of Light , propagating in the radial – direction

with the speed of light $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$.

The input for the Electric Field Intensity $\{E(x, y, z) = ey\}$ and the Magnetic Field

for the Electromagnetic Field within a constant gravitational field with acceleration

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}) + \frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) \mathbf{g}$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) \mathbf{g}$$

Equation (73) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} + \text{term6} = 0$$

In[]:= $\epsilon_0 =$

```
In[ ]:=  $\mu_0 =.$ 
```

```
In[ ]:= x =.
```

```
In[ ]:= y =.
```

```
In[ ]:= z =.
```

```
In[ ]:= t =.
```

```
In[ ]:= Get["VectorAnalysis`"]
```

— **General**: VectorAnalysis` is now obsolete. The legacy version being loaded may conflict with

```
In[ ]:= Get["Calculus`DSolve`"]
```

— **Get**: Cannot open Calculus`DSolve`.

```
Out[ ]:= $Failed
```

```
In[ ]:= InverseFunctions → True
```

```
Out[ ]:= InverseFunctions → True
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[ ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:= Get["Calculus`DSolveIntegrals`"]
```

— **Get**: Cannot open Calculus`DSolveIntegrals`.

```
Out[ ]:= $Failed
```

```
In[ ]:= SetCoordinates[Cartesian[x, y, z]]
```

```
Out[ ]:= Cartesian[x, y, z]
```

```
In[ ]:= G1 = .
```

```
In[ ]:=  $\epsilon_0$  = .
```

```
In[ ]:=  $\mu_0$  =.
```

```
In[ ]:= fg = .
```

```
In[ ]:= Msun = .
```

The energy from the Sun - both heat and light energy - originates from a specific type of fusion that occurs inside of the Sun (known as proton-proton fusion, or simply a lone hydrogen nucleus) and through a series of steps, these protons fuse together to form helium. This process occurs inside the core of the Sun, and the transformation results in a release of energy that moves out from the Core of the Sun and moves across the solar system.[3] It is important to note that the core is the only significant amount of heat through fusion (it contributes about 99% of the total energy of the core).

It is not clear from which part of the sun the GRS spectra has been measured. It is assumed to be emitted from the exact center of the sun ($z_1 = 0$) until the part of the core that is closest to the surface.

The energy from the Sun, both heat and light energy, originates from a nuclear fusion process that is occurring inside the core. The type of fusion that occurs inside of the Sun is known as proton-proton fusion.

Inside the Sun, this process begins with protons (which is simply a lone hydrogen nucleus). These protons fuse together and are turned into helium. This fusion process and the transformation results in a release of energy that keeps the sun from cooling down and moves across the solar system. It is important to note that the core is the only significant amount of heat through fusion (it contributes about $99 \times \%$). The rest of the Sun's energy is produced by the outer layers of the sun.

The sun looks like a featureless yellow orb from Earth,

but it has discrete internal layers. The central core, which is the only place where nuclear fusion happens, extends to a radius of 138 000 kilometers. Beyond that, the radiative zone and the convective zone reaches to the photosphere. At a radius of 695 000 kilometers, the photosphere is the deepest layer that astronomers can observe directly.

Inside the Gravitational Radius of the Sun

(the distance of the center of the sun where the gravitational acceleration of the sun changes from increasing into decreasing)

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$

oppositely directed towards the gravitational acceleration within the sun. The gravitational acceleration within the fusion core of the sun will increase with the distance r .

$$g_1[r] = K_1 r = f_g \frac{M_{\text{Sun}}}{4 \pi (\text{Radius}_{\text{Sun}})^3} r$$

within a Radial Gravitational Field $g[r]$ oriented in the radial –direction of the Sun with acceleration $g_1[r]$ resulting in the Gravitational Redshift caused by the Gravitational Field within the fusion core.

The Gravitational Intensity Shift for the light emitted by the sun equals

$$I_{\text{NGR}} = e^{-\frac{1}{2} K_1 \epsilon_0 \mu_0 z^2}$$

Instead of Spherical Coordinates (r, θ, φ) for the light emitted Spherically for the far field (within a small area like the dimensions of a Space Telescope) Cartesian Coordinates (x, y, z) are being used.

$$\ln[\bullet] := \epsilon_0 = .$$

$$\ln[\bullet] := \mu_0 = .$$

In[•]:= fg = .

In[•]:= Msun = .

In[•]:= K1 = .

In[•]:= K2 = .

In[•]:= $h[z] = K2 e^{-\frac{1}{4} K1 z^2 \epsilon_0 \mu_0}$

Out[•]:= $e^{-\frac{1}{4} K1 z^2 \epsilon_0 \mu_0} K2$

In[•]:= $ev = \{h[z] \times g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}], 0, 0\}$

Out[•]:= $\{e^{-\frac{1}{4} K1 z^2 \epsilon_0 \mu_0} K2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}], 0, 0\}$

In[•]:= $mv = (1/\text{Sqrt}[\mu_0]) * \text{Sqrt}[\epsilon_0] * \{0, h[z] \times g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}], 0\}$

Out[•]:= $\{0, \frac{e^{-\frac{1}{4} K1 z^2 \epsilon_0 \mu_0} K2 \sqrt{\epsilon_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}}, 0\}$

In[•]:= $gv = \{0, 0, K1 z\}$

Out[•]:= $\{0, 0, K1 z\}$

In[•]:= $\text{Intensity} = -\frac{1}{2} (\epsilon_0 (\text{Dot}[ev, ev]) + \mu_0 (\text{Dot}[mv, mv]))$

Out[•]:= $-\frac{1}{2} \left(e^{-\frac{1}{2} K1 z^2 \epsilon_0 \mu_0} K2^2 \epsilon_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 + e^{-\frac{1}{2} K1 z^2 \epsilon_0 \mu_0} K2^2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 \epsilon_0 \right)$

In[]:= FullSimplify[%]

$$\text{Out[]} = -\frac{e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 \mathbf{1} (\epsilon_0 + \epsilon_0)}{2}$$

In[]:= Div[ev]

$$\text{Out[]} = 0$$

In[]:= Div[mv]

$$\text{Out[]} = 0$$

In[]:= FullSimplify[%]

$$\text{Out[]} = 0$$

In[]:= term1a = D[Cross[ev, mv], t]

$$\text{Out[]} = \left\{ 0, 0, \frac{2 e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \sqrt{\epsilon_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}} \right\}$$

In[]:=

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}.$$

In[]:= term1 = ((-epsilon0)*mu0)*D[Cross[ev, mv], t]

$$\text{Out[]} = \left\{ 0, 0, -2 e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \epsilon_0^{3/2} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right\}$$

In[]:=

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}).$$

In[]:= term2 = epsilon0*ev*Div[ev]

$$\text{Out[]} = \{0, 0, 0\}$$

In[•]:=

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}).$$

In[•]:= term3 = (-ε0)*Cross[ev, Curl[ev]]

$$\text{Out[•]} = \left\{ 0, 0, -\epsilon_0 \left(-\frac{1}{2} e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_1 k_2^2 z \epsilon_0 \mu_0 g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 - e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \sqrt{\epsilon_0} \sqrt{\mu_0} \right) \right\}$$

In[•]:=

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}).$$

In[•]:= term4 = μ0*mv*Div[mv]

$$\text{Out[•]} = \{0, 0, 0\}$$

In[•]:=

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}).$$

In[•]:= term5 = (-μ0)*Cross[mv, Curl[mv]]

$$\text{Out[•]} = \left\{ 0, 0, -\mu_0 \left(-\frac{1}{2} e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_1 k_2^2 z \epsilon_0^2 g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 - \frac{e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \epsilon_0^{3/2} g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2}{2} \right) \right\}$$

In[•]:=

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) \mathbf{g}.$$

In[•]:= term6 = -\left(\frac{\epsilon^2 \mu_0}{2} \text{Dot}[ev, ev] + \frac{\epsilon_0 \mu_0^2}{2} \text{Dot}[mv, mv] \right) gv

$$\text{Out[•]} = \left\{ 0, 0, -e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_1 k_2^2 z \epsilon_0^2 \mu_0 g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 \right\}$$

`In[]:=` vergelijking = term1 + term2 + term3 + term4 + term5 + term6

$$\text{Out[]} = \left\{ \theta, \theta, -e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_1 k_2^2 z \epsilon_0^2 \mu_0 g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 - 2 e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \epsilon_0^{3/2} \sqrt{\mu_0} g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 - \frac{e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \epsilon_0^{3/2} g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2}{\sqrt{\mu_0}} \right. \\ \left. \mu_0 \left(-\frac{1}{2} e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_1 k_2^2 z \epsilon_0^2 g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 - \frac{e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \epsilon_0^{3/2} g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2}{\sqrt{\mu_0}} \right) \right. \\ \left. \epsilon_0 \left(-\frac{1}{2} e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_1 k_2^2 z \epsilon_0 \mu_0 g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 - e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \sqrt{\epsilon_0} \sqrt{\mu_0} g \left[t - z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 \right) \right.$$

`In[]:=`

The electromagnetic force density in the x - direction equals :

`In[]:=` xvergelijking = term1[[1]] + term2[[1]] + term3[[1]] + term4[[1]] + term5[[1]] + term6[[1]]

`Out[]:=` 0

`In[]:=` FullSimplify[%]

`Out[]:=` 0

`In[]:=` xvergelijking1 = %

`Out[]:=` 0

`In[]:=`

The electromagnetic force density in the y - direction equals :

`In[]:=` yvergelijking = term1[[2]] + term2[[2]] + term3[[2]] + term4[[2]] + term5[[2]] + term6[[2]]

`Out[]:=` 0

`In[]:=` FullSimplify[%]

`Out[]:=` 0

`In[]:=` yvergelijking1 = %

`Out[]:=` 0

In[•]:=

The electromagnetic force density in the z - direction equals :

In[•]:= zvergelijking = term1[[3]] + term2[[3]] + term3[[3]] + term4[[3]] +
term5[[3]] + term6[[3]]

Out[•]:=
$$-e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_1 k_2^2 z \epsilon_0^2 \mu_0 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 - 2 e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \epsilon_0^{3/2} \sqrt{\mu_0} g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]$$

$$\mu_0 \left(-\frac{1}{2} e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_1 k_2^2 z \epsilon_0^2 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 - \frac{e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \epsilon_0^{3/2} g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}} \right)$$

$$\epsilon_0 \left(-\frac{1}{2} e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_1 k_2^2 z \epsilon_0 \mu_0 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 - e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \sqrt{\epsilon_0} \sqrt{\mu_0} g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right)$$

In[•]:= FullSimplify[%]

Out[•]:= 0

In[•]:= zvergelijking1 = %

Out[•]:= 0

Results force densities in resp x-direction, y-direction, z-direction

Results for the electromagnetic force densities in resp x-direction, y-direction, z-direction:

In[•]:= xvergelijking1

Out[•]:= 0

In[•]:= yvergelijking1

Out[•]:= 0

In[•]:= zvergelijking1

Out[•]:= 0

According the force-density equations in the x-direction, y-
equals zero in every direction. This represents the solution for ϵ_0
It follows from the mathematical solution for the electromagnetic
that the **intensity increases** with the value:

$$\text{Intensity} = -\frac{1}{2} (\epsilon_0 (\text{Dot}[ev, ev]) + \mu_0 (\text{Dot}[mv, mv]))$$

$$= \frac{1}{2} \left(e^{-\frac{1}{4} K_1 z^2 \epsilon_0 \mu_0} \epsilon_0 g \left[e^{-\frac{1}{2} K_1 z^2 \epsilon_0 \mu_0} (t-z \sqrt{\epsilon_0} \sqrt{\mu_0}) \right]^2 + e^{-\frac{1}{4} K_1 z^2 \epsilon_0 \mu_0} g \left[e^{-\frac{1}{2} K_1 z^2 \epsilon_0 \mu_0} (t-z \sqrt{\epsilon_0} \sqrt{\mu_0}) \right]^2 \right)$$

The Electromagnetic Energy Intensity is proportional to: $e^{-\frac{1}{2} K_1 z^2 \epsilon_0 \mu_0}$
 distance z in the direction **opposite** to the z -direction of the grav

The frequency is proportional to the energy density ([book: Equation](#)
 energy. The speed of light remains **constant** in a gravitational f

Within a Constant Gravitational Field $K_1 z$ The observed Cosm

$$\omega_{\text{NLGR}} = \omega_0 e^{-\frac{1}{2} K_1 z^2 \epsilon_0 \mu_0} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

The term $\left(\frac{\Delta \omega}{\omega} = e^{-\frac{1}{2} K_1 z^2 \epsilon_0 \mu_0} \right)$

has been presented in generally as a **GRS** Redshift comparable
 generated by a velocity v_{Doppler} :

$$v_{\text{Doppler}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}]$$

There are two types of **GRS** generated by the sun.

1) GRS generated inside the sun where the gravitational field is

$g[z] = G_1 z$ with the Solution:

$$v_{\text{Doppler-1}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{1}{2} G_1 z^2 \mu_0 \epsilon_0}$$

([book, page 64, Equation \(111\)](#))

2) GRS generated outside the sun where the gravitational field
 to the radial distance $\frac{1}{z^2} g[z] = G_1 \frac{1}{z^2}$ with the Solution:

$$v_{\text{Doppler-2}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-g z \mu_0 \epsilon_0}$$

(book, page 64, Equation (111))

$$\text{In}[] := \text{Intensity} = -\frac{1}{2} \left(\epsilon_0 (\text{Dot}[ev, ev]) + \mu_0 (\text{Dot}[mv, mv]) \right)$$

$$\text{Out}[] = -\frac{1 \left(e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 \epsilon_0 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 + e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 \epsilon_0 \right)}{2}$$

$$\text{In}[] := \text{FullSimplify}[\%]$$

$$\text{Out}[] = -\frac{e^{-\frac{1}{2} k_1 z^2 \epsilon_0 \mu_0} k_2^2 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 1 (\epsilon_0 + \epsilon_0)}{2}$$

1) GRS generated inside the sun where the gravitational field is

$g[z] = G_1 z$ with the Solution:

$$v_{\text{Doppler-1}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{1}{2} G_1 z^2 \mu_0 \epsilon_0}$$

(book, page 64, Equation (111))

$$v_{\text{Doppler-1}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{1}{2} G_1 z_2^2 \mu_0 \epsilon_0} - c e^{-\frac{1}{2} G_1 z_1^2 \mu_0 \epsilon_0}$$

With:

$z_1 =$ Center of the Fusion core within the sun ($z_1 = 0$)

$z_2 =$ Radius of the sun ($z_2 = 696\,340 \times 10^3$)

$$\text{In}[] := c = 3 \times 10^8$$

$$\text{Out}[] = 300\,000\,000$$

$$\text{In}[] := \epsilon_0 = 8.85 \times 10^{-12}$$

$$\text{Out}[] = 8.85 \times 10^{-12}$$

`In[]:= $\mu_0 = 4 \pi 10^{-7}$`

`Out[]= $\frac{\pi}{2500000}$`

`In[]:= $fg = 6.67428 \times 10^{-11}$`

`Out[]= 6.67428×10^{-11}`

`In[]:= $M_{\text{sun}} = 1.98847 10^{30}$`

`Out[]= 1.98847×10^{30}`

`In[]:= $R_{\text{sun}} = 696340 10^3$`

`Out[]= 696340000`

`In[]:= $K1 = \frac{fg M_{\text{sun}}}{4 \pi R_{\text{sun}}^3}$`

`Out[]= 3.12788×10^{-8}`

`In[]:= $z1 = 0$`

`Out[]= 0`

`In[]:= $z2 = 696340 10^3$`

`Out[]= 696340000`

`In[]:= $g[z] = K1 z$`

`Out[]= $3.12788 \times 10^{-8} z$`

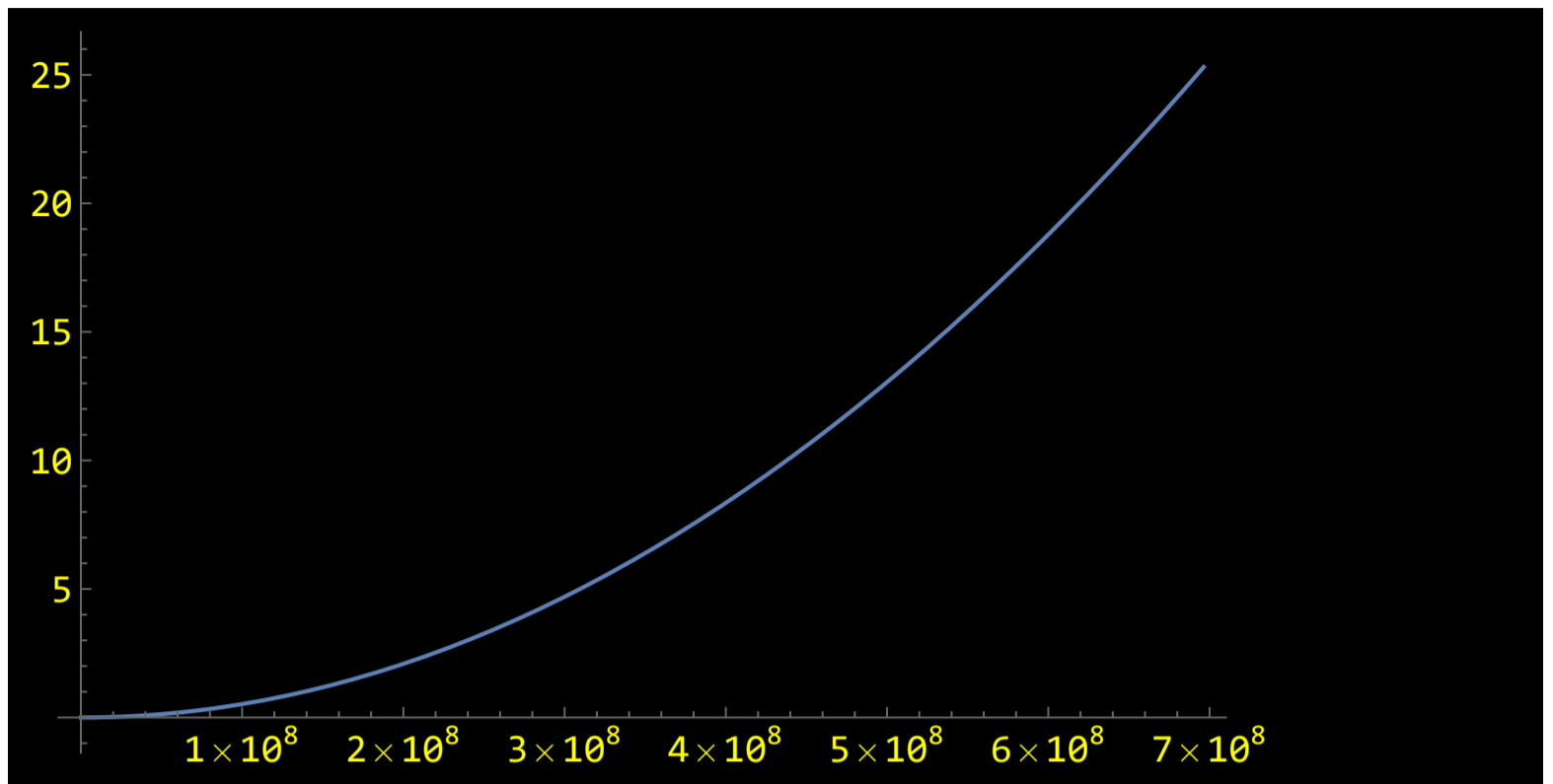
`In[]:= $g[z] = K1 z$`

`Out[]= $3.12788 \times 10^{-8} z$`

The Gravitational Doppler Shift from the center of the sun until the Gravitational

In[•]:= $\text{Plot}\left[c \left(e^{-\frac{1}{2} K_1 z_1^2 \mu_0 \epsilon_0} - e^{-\frac{1}{2} K_1 z_2^2 \mu_0 \epsilon_0} \right), \{z, 0, z_2\}\right]$

Out[•]:=



In[•]:= $v_{\text{Doppler}} = c \left(e^{-\frac{1}{2} K_1 z_1^2 \mu_0 \epsilon_0} - e^{-\frac{1}{2} K_1 z_2^2 \mu_0 \epsilon_0} \right)$

Out[•]:= 25.3009

The difference between the observed **GRS** of the light of the sun in the center of the sun ($z_1 = 0$) until the radius of the sun ($z_2 = 696\,340$)

Example 5

Propagation of a Beam of Light in the radial-direction of the **Sirius** from the Gravitational Radius of **Sirius** until with the speed of light $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$ within a Radial Gravitational Field G_1 oriented in the radial direction resulting in Gravitational Redshift $v_{\text{Grav}-1}$ (GRS) caused

There are **two** kinds of Redshift caused by the gravitational field of the

- 1) Redshift₁ caused by the Gravitational Field within the **fusion core** (created). This has been calculated in Example 3
- 2) Redshift₂ caused by the Gravitational Field outside the fusion core

The total RedShift caused by the Gravitational Field of the sun is the

Book : [Rising of the James Webb Space Telescope and its Fundamental Bl](#)

Example of a Spherical Beam of Light , propagating in the radial – direction

with the speed of light $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$.

The input for the Electric Field Intensity $\{E(x, y, z) = ev\}$ and the Magnetic Field Intensity $\{H(x, y, z) = hv\}$ for the Electromagnetic Field within a constant gravitational field with acceleration g .

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}) + \frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) \mathbf{g}$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) \mathbf{g}$$

Equation (73) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} + \text{term6} = 0$$

```
In[• ]:=  $\epsilon_0 =.$ 
```

```
In[• ]:=  $\mu_0 =.$ 
```

```
In[• ]:=  $x =.$ 
```

```
In[• ]:=  $y =.$ 
```

```
In[• ]:=  $z =.$ 
```

```
In[• ]:=  $t =.$ 
```

```
In[• ]:= Get["VectorAnalysis`"]
```

— **General**: VectorAnalysis` is now obsolete. The legacy version being loaded may conflict wit

```
In[• ]:= Get["Calculus`DSolve`"]
```

— **Get**: Cannot open Calculus`DSolve`.

```
Out[• ]:= $Failed
```

```
In[• ]:= InverseFunctions → True
```

```
Out[• ]:= InverseFunctions → True
```

```
In[• ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[• ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[• ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:= Get["Calculus`DSolveIntegrals`"]
```

—  **Get**: Cannot open Calculus`DSolveIntegrals`.

```
Out[ ]:= $Failed
```

```
In[ ]:= SetCoordinates[Cartesian[x, y, z]]
```

```
Out[ ]:= Cartesian[x, y, z]
```

```
In[ ]:= G1 = .
```

```
In[ ]:=  $\epsilon_0$  = .
```

```
In[ ]:=  $\mu_0$  = .
```

```
In[ ]:= fg = .
```

```
In[ ]:= Msun = .
```


The light being emitted by the sun has been created by **nuclear fusion in the core**

Outside the **Gravitational Radius** of the Sun, (the distance of the center of the sun where the generated light will propagate with the speed of light :

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$

oppositely directed towards the gravitational acceleration outside the sun. The gravitational acceleration outside the sun will increase proportionally

$$g_2[r] = K_2 \frac{1}{r^2} = \frac{f_g M_{\text{Sun}}}{4 \pi} \frac{1}{r^2}$$

within a **Radial Gravitational Field** $g[r]$ oriented

in the radial – direction of the **Sun** with **acceleration** $g[r]$ resulting in the

Gravitational Redshift caused by the **Gravitational Field outside the Sun**.

The **Gravitational Intensity Shift** for the light emitted by the sun equals

$$I_{\text{NGR}} = e^{-\frac{K_2 \epsilon_0 \mu_0}{z}}$$

Instead of Spherical Coordinates (r, θ, φ) for the light emitted Spherically

for the far field (within a small area like the dimensions of a **Space Telescope**)

Cartesian Coordinates (x, y, z) are being used.

$$\text{In}[\bullet] := \epsilon_0 = .$$

$$\text{In}[\bullet] := \mu_0 = .$$

$$\text{In}[\bullet] := f_g = .$$

`In[•]:= Msun = .`

`In[•]:= K1 = .`

`In[•]:= K2 = .`

`In[•]:= h[z] = K3 e- $\frac{K2 \epsilon_0 \mu_0}{2z}$ }`

`Out[•]:= e- $\frac{K2 \epsilon_0 \mu_0}{2z}$ } K3`

`In[•]:= ev = {h[z] × g[t - z √ ϵ_0 √ μ_0], 0, 0}`

`Out[•]:= {e- $\frac{K2 \epsilon_0 \mu_0}{2z}$ } K3 g[t - z √ ϵ_0 √ μ_0], 0, 0}`

`In[•]:= mv = (1/Sqrt[μ_0]) * Sqrt[ϵ_0] *
{0, h[z] × g[t - z √ ϵ_0 √ μ_0], 0}`

`Out[•]:= {0, $\frac{e^{-\frac{K2 \epsilon_0 \mu_0}{2z}} K3 \sqrt{\epsilon_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}}$, 0}`

`In[•]:= g2 = {0, 0, $-\frac{K2}{z^2}$ }`

`Out[•]:= {0, 0, $-\frac{K2}{z^2}$ }`

`In[•]:= Intensity = $\frac{1}{2}$ (ϵ_0 (Dot[ev, ev]) + μ_0 (Dot[mv, mv]))`

`Out[•]:= $\frac{1}{2} \left(e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 \epsilon_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 + e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 \epsilon_0 \right)$`

2

In[•]:= FullSimplify[%]

$$\text{Out[•]} = \frac{e^{-\frac{k^2 \epsilon_0 \mu_0}{z}} k^3 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 \mathbf{1} (\epsilon_0 + \epsilon_0)}{2}$$

In[•]:= Div[ev]

$$\text{Out[•]} = 0$$

In[•]:= Div[mv]

$$\text{Out[•]} = 0$$

In[•]:= FullSimplify[%]

$$\text{Out[•]} = 0$$

In[•]:= term1a = D[Cross[ev, mv], t]

$$\text{Out[•]} = \left\{ 0, 0, \frac{2 e^{-\frac{k^2 \epsilon_0 \mu_0}{z}} k^3 \sqrt{\epsilon_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}} \right\}$$

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

In[•]:= term1 = ((-ε0)*μ0)*D[Cross[ev, mv], t]

$$\text{Out[•]} = \left\{ 0, 0, -2 e^{-\frac{k^2 \epsilon_0 \mu_0}{z}} k^3 \epsilon_0^{3/2} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right\}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

In[•]:= term2 = ε0*ev*Div[ev]

$$\text{Out[•]} = \{0, 0, 0\}$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

In[]:= term3 = (-ε0)*Cross[ev, Curl[ev]]

$$\text{Out[]} = \left\{ 0, 0, -\epsilon_0 \left(\frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_3^2 \sqrt{\epsilon_0} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right) \right\}$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

In[]:= term4 = μ0 * mv * Div[mv]

$$\text{Out[]} = \{0, 0, 0\}$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

In[]:= term5 = (-μ0)*Cross[mv, Curl[mv]]

$$\text{Out[]} = \left\{ 0, 0, -\mu_0 \left(\frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0^2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - \frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_3^2 \epsilon_0^{3/2} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}} \right) \right\}$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\overline{\mathbf{E} \cdot \mathbf{E}} \right) + \epsilon \mu^2 \left(\overline{\mathbf{H} \cdot \mathbf{H}} \right) \right) g$$

In[]:= term6 = -\left(\frac{\epsilon_0^2 \mu_0}{2} \text{Dot}[ev, ev] + \frac{\epsilon_0 \mu_0^2}{2} \text{Dot}[mv, mv] \right) g^2

$$\text{Out[]} = \left\{ 0, 0, \frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0^2 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{z^2} \right\}$$

In[]:= vergelijking = term1 + term2 + term3 + term4 + term5 + term6

$$\text{Out[]} = \left\{ 0, 0, \frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0^2 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{z^2} - 2 e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_3^2 \epsilon_0^{3/2} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right. \\ \left. \mu_0 \left(\frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0^2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - \frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_3^2 \epsilon_0^{3/2} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}} \right) \right. \\ \left. \epsilon_0 \left(\frac{e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_2 k_3^2 \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - e^{-\frac{k_2 \epsilon_0 \mu_0}{z}} k_3^2 \sqrt{\epsilon_0} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right) \right\}$$

In[•]:=

The electromagnetic force density in the x - direction equals :

In[•]:= xvergelijking = term1[1] + term2[1] + term3[1] + term4[1] +
term5[1] + term6[1]

Out[•]= 0

In[•]:= FullSimplify[%]

Out[•]= 0

In[•]:= xvergelijking1 = %

Out[•]= 0

In[•]:=

The electromagnetic force density in the y - direction equals :

In[•]:= yvergelijking = term1[2] + term2[2] + term3[2] + term4[2] +
term5[2] + term6[2]

Out[•]= 0

In[•]:= FullSimplify[%]

Out[•]= 0

In[•]:= yvergelijking1 = %

Out[•]= 0

The electromagnetic force density in the z - direction equals :

In[•]:= zvergelijking = term1[3] + term2[3] + term3[3] + term4[3] +
term5[3] + term6[3]

$$\text{Out[•]} = \frac{e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K2 K3^2 \epsilon_0^2 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{z^2} - 2 e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 \epsilon_0^{3/2} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \epsilon_0$$

$$\mu_0 \left(\frac{e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K2 K3^2 \epsilon_0^2 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - \frac{e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 \epsilon_0^{3/2} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}} \right)$$

$$\epsilon_0 \left(\frac{e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K2 K3^2 \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2}{2 z^2} - e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 \sqrt{\epsilon_0} \sqrt{\mu_0} g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right)$$

In[•]:= FullSimplify[%]

Out[•]= 0

In[•]:= zvergelijking1 = %

Out[•]= 0

Results for the electromagnetic force densities in resp x-direction, y-direction, z-direction:

In[•]:= xvergelijking1

Out[•]= 0

In[•]:= yvergelijking1

Out[•]= 0

In[•]:= zvergelijking1

Out[•]= 0

According the force-density equations in the x-direction, y-direction and z-direction, the force-density is zero in every direction. This represents the solution for equation (73) on page 53. It follows from the mathematical solution for the electromagnetic field

$$E_v = e^{-\frac{K2 \epsilon_0 \mu_0}{z}} g \left[e^{-\frac{K2 \epsilon_0 \mu_0}{2z}} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0}) \right]$$

that the **intensity increases** with the value:

$$\text{Intensity} = \frac{1}{2} (\epsilon_0 (\text{Dot}[ev, ev]) + \mu_0 (\text{Dot}[mv, mv])) =$$

$$= e^{-\frac{K_2 \epsilon_0 \mu_0}{z}} \epsilon_0 g \left[e^{-\frac{K_2 \epsilon_0 \mu_0}{2z}} (t - z \sqrt{\epsilon_0} \sqrt{\mu_0}) \right]^2$$

The Electromagnetic Energy Intensity is proportional to: $e^{-\frac{K_2 \epsilon_0 \mu_0}{z}}$ along distance z in the direction **opposite** to the z -direction of the gravitation

The frequency is proportional to the energy density ([book: Equation 98 Page](#))

The speed of light remains **constant** in a gravitational field.

Within a Gravitational Field $\frac{K_2}{z^2}$ The observed Cosmological Redshift

$$\omega_{\text{NLGR}} = \omega_0 e^{-\frac{K_2 \epsilon_0 \mu_0}{z}} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

$$\text{The term } \left(\frac{\Delta \omega}{\omega} = e^{-\frac{K_2 \epsilon_0 \mu_0}{z}} \right)$$

has been presented in generally as a **GRS** Redshift comparable with the generated by a velocity v_{Doppler} :

$$v_{\text{Doppler}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{K_2 \epsilon_0 \mu_0}{z}}$$

There are two types of **GRS** generated by the sun.

1) GRS generated inside the sun where the gravitational field is proportional

$g[z] = K_1 z$ with the Solution:

$$v_{\text{Doppler-1}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{1}{4} K_1 z^2 \mu_0 \epsilon_0}$$

([book, page 64, Equation \(111\)](#))

2) GRS generated outside the sun where the gravitational field is proportional to the radial distance $\frac{1}{z^2}$

$g[z] = K_2 \frac{1}{z^2}$ with the Solution:

$$v_{\text{Doppler-2}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{K2 \epsilon_0 \mu_0}{z}}$$

(book, page 64, Equation (111))

$$\text{In}[] := \text{Intensity} = -\frac{1}{2} (\epsilon_0 (\text{Dot}[\text{ev}, \text{ev}]) + \mu_0 (\text{Dot}[\text{mv}, \text{mv}]))$$

$$\text{Out}[] = -\frac{1 \left(e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 \epsilon_0 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 + e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 \epsilon_0 \right)}{2}$$

$$\text{In}[] := \text{FullSimplify}[\%]$$

$$\text{Out}[] = -\frac{e^{-\frac{K2 \epsilon_0 \mu_0}{z}} K3^2 g [t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]^2 1 (\epsilon_0 + \epsilon_0)}{2}$$

2) GRS generated outside the sun where the gravitational field to the radial distance $\frac{1}{z^2}$

$g[z] = K2 \frac{1}{z^2}$ with the Solution:

$$v_{\text{Doppler-2}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{K2 \epsilon_0 \mu_0}{z}}$$

(book, page 64, Equation (111))

$$v_{\text{Doppler-1}} = c \frac{\Delta \omega}{\omega} [\text{m s}^{-1}] = c e^{-\frac{K2 \epsilon_0 \mu_0}{z_2}} - c e^{-\frac{K2 \epsilon_0 \mu_0}{z_1}}$$

With:

$z_1 =$ Radius of the sun

$z_2 =$ Distance between the sun and the Earth

$$\text{In}[] := c = 3 \times 10^8$$

$$\text{Out}[] = 300000000$$

`In[]:=` $\epsilon_0 = 8.85 \times 10^{-12}$

`Out[]:=` 8.85×10^{-12}

`In[]:=` $\mu_0 = 4 \pi 10^{-7}$

`Out[]:=` $\frac{\pi}{2500000}$

`In[]:=` $fg = 6.67428 \times 10^{-11}$

`Out[]:=` 6.67428×10^{-11}

`In[]:=` $M_{\text{sun}} = 1.98892 \times 10^{30}$

`Out[]:=` 1.98892×10^{30}

`In[]:=` $M_{\text{SiriusB}} = 1.018 M_{\text{sun}}$

`Out[]:=` 2.02472×10^{30}

`In[]:=` $R_{\text{Sun}} = 69634000$

`Out[]:=` 69634000

`In[]:=` $R_{\text{SiriusB}} = 1.711 R_{\text{Sun}}$

`Out[]:=` 1.19144×10^8

`In[]:=` $\text{Lightyear} = 9.461 \times 10^{15}$

`Out[]:=` 9.461×10^{15}

`In[]:=` $z_2 = 8.611 \text{ Lightyear}$

`Out[]:=` 8.14687×10^{16}

$$\text{In}[] := K2 = \frac{f_g M_{\text{SiriusB}}}{4 \pi}$$

$$\text{Out}[] = 1.07537 \times 10^{19}$$

$$\text{In}[] := z1 = 0.0063875 R_{\text{Sun}}$$

$$\text{Out}[] = 444787.$$

The distance between Sirius and Earth equals z2

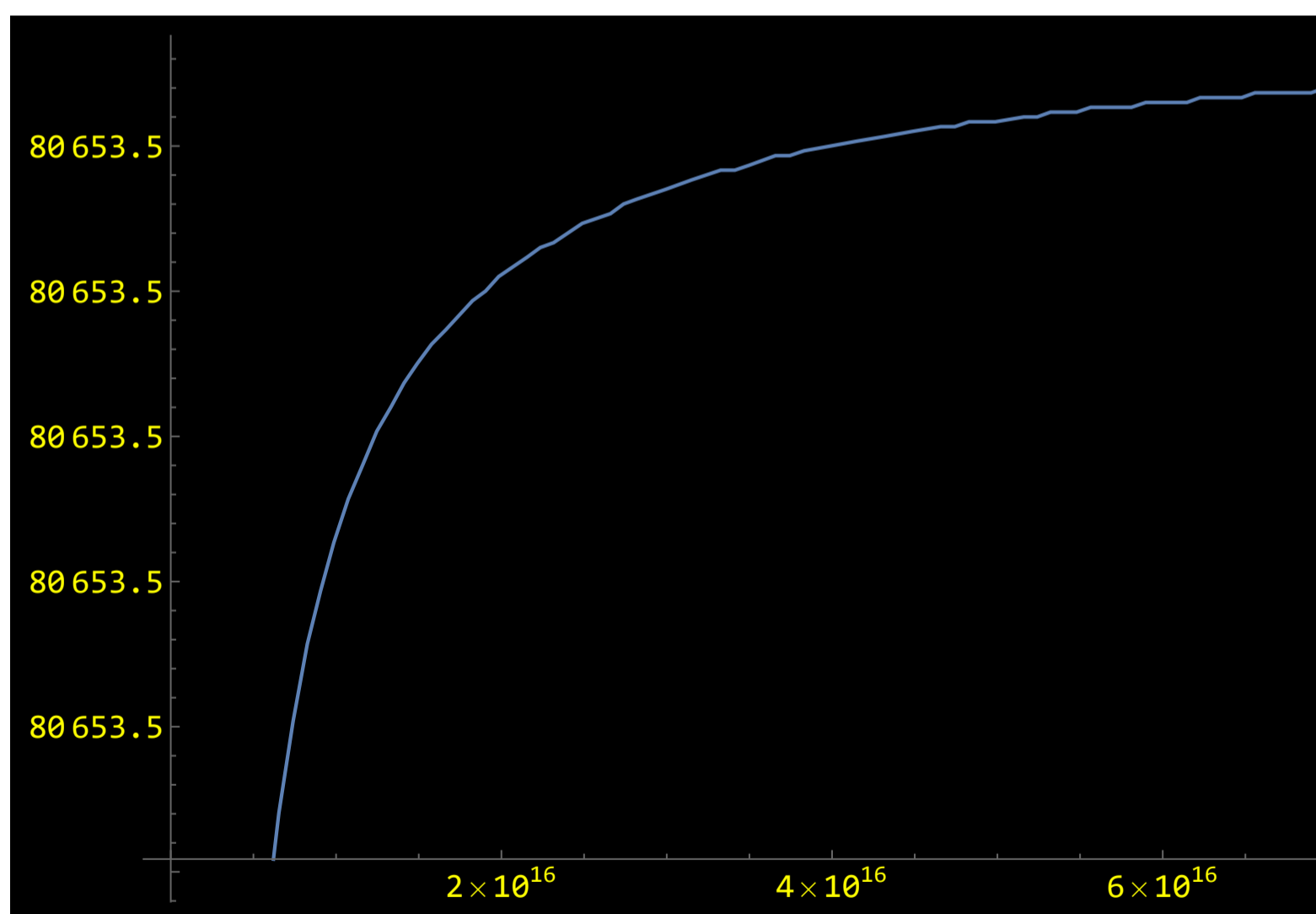
$$\text{In}[] := z2 = 8.611 \text{ Lightyear}$$

$$\text{Out}[] = 8.14669 \times 10^{16}$$

The Gravitational RedShift from the "Intense Emitting Radiation Radius z

$$\text{In}[] := \text{Plot}\left[c \left(e^{-\frac{K2 \epsilon_0 \mu_0}{z}} - e^{-\frac{K2 \epsilon_0 \mu_0}{z1}} \right), \{z, z1, z2\}\right]$$

$$\text{Out}[] =$$



$$\text{In}[] := v_{\text{Doppler}} = c \left(e^{-\frac{K2 \epsilon_0 \mu_0}{z2}} - e^{-\frac{K2 \epsilon_0 \mu_0}{z1}} \right)$$

$$\text{Out}[] = 597.538$$

The calculated value of 80.65 k[m/s] for the GRS of the Sun corresponds to the measured average value for the GRS of published in :

[The gravitational redshift of Sirius B](#)

Example 6

The Gravitational Wave Equation.

Propagation of a Gravitational Wave in the z-direction with

speed of light: $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$

In[•]:=

Book : [Rising of the James Webb Space Telescope and its Fundamental](#)

Example of a Spherical Beam of Light , propagating in the radial – direction

with the speed of light $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$.

The input for the Electric Field Intensity $\{E(x, y, z, t) = ev\}$ and the Magnetic Field Intensity $\{H(x, y, z, t) = ev\}$ into the Poynting Equation for the Electromagnetic Field within a constant gravitational field with a constant metric tensor $g_{\mu\nu}$.

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}) + \frac{1}{2} \left(\epsilon_0^2 \mathbf{E} \cdot \mathbf{E} + \mu_0^2 \mathbf{H} \cdot \mathbf{H} \right)$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \overline{\mathbf{H}} \times (\nabla \times \overline{\mathbf{H}})$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\overline{\mathbf{E}} \cdot \overline{\mathbf{E}} \right) + \epsilon \mu^2 \left(\overline{\mathbf{H}} \cdot \overline{\mathbf{H}} \right) \right) \overline{\mathbf{g}}$$

Equation (73) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} + \text{term6} = 0$$

`In[•]:=` `ϵ0 =.`

`In[•]:=` `μ0 =.`

`In[•]:=` `x =.`

`In[•]:=` `y =.`

`In[•]:=` `z =.`

`In[•]:=` `t =.`

`In[•]:=` `Get["VectorAnalysis`"]`

— **General**: VectorAnalysis` is now obsolete. The legacy version being loaded may conflict wit

`In[•]:=` `Get["Calculus`DSolve`"]`

— **Get**: Cannot open Calculus`DSolve`.

`Out[•]:=` `$Failed`

`In[•]:=` `InverseFunctions → True`

`Out[•]:=` `InverseFunctions → True`

```
In[ ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[ ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:= Get["Calculus`DSolveIntegrals`"]
```

—  **Get**: Cannot open Calculus`DSolveIntegrals`.

```
Out[ ]:= $Failed
```

```
In[ ]:= SetCoordinates[Cartesian[x, y, z]]
```

```
Out[ ]:= Cartesian[x, y, z]
```

```
In[ ]:= {Coordinates[Cartesian], CoordinateRanges[Cartesian]}
```

```
Out[ ]:= {{x, y, z}, {-∞ < x < ∞, -∞ < y < ∞, -∞ < z < ∞}}
```

```
In[ ]:= G1 = .
```

```
In[ ]:= h[x, y, z, t] = e-1/2 z √ε₀ μ₀ g[t-z √ε₀ √μ₀] f[t - z √ε₀ √μ₀, x, y]
```

```
Out[ ]:= e-1/2 z √ε₀ μ₀ g[t-z √ε₀ √μ₀] f[t - z √ε₀ √μ₀, x, y]
```

```
In[ ]:= ev = {h[x, y, z, t], 0, 0}
```

```
Out[ ]:= {e-1/2 z √ε₀ μ₀ g[t-z √ε₀ √μ₀] f[t - z √ε₀ √μ₀, x, y], 0, 0}
```

```
In[ ]:= mv = (1/Sqrt[μ₀])*Sqrt[ε₀]*
{0, h[x, y, z, t], 0}
```

```
Out[ ]:= {0,  $\frac{e^{-\frac{1}{2} z \sqrt{\epsilon_0} \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \sqrt{\epsilon_0} f[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]}{\sqrt{\mu_0}}$ , 0}
```

$$\text{In}[] := \mathbf{gv} = \{0, 0, g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]\}$$

$$\text{Out}[] = \{0, 0, g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]\}$$

$$\text{In}[] := \text{Intensity} = -\frac{1}{2} (\epsilon_0 (\text{Dot}[\mathbf{ev}, \mathbf{ev}]) + \mu_0 (\text{Dot}[\mathbf{mv}, \mathbf{mv}]))$$

$$\text{Out}[] = -\frac{1 \left(e^{-z \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0 f[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 + e^{-z \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]} f[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 \right)}{2}$$

$$\text{In}[] := \text{FullSimplify}[\%]$$

$$\text{Out}[] = -\frac{e^{-z \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]} f[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 1 (\epsilon_0 + \epsilon_0)}{2}$$

$$\text{In}[] := \text{Div}[\mathbf{ev}]$$

$$\text{Out}[] = e^{-\frac{1}{2} z \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]} f^{(0,1,0)}[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]$$

$$\text{In}[] := \text{Div}[\mathbf{mv}]$$

$$\text{Out}[] = \frac{e^{-\frac{1}{2} z \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \sqrt{\epsilon_0} f^{(0,0,1)}[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]}{\sqrt{\mu_0}}$$

$$\text{In}[] := \text{FullSimplify}[\%]$$

$$\text{Out}[] = \frac{e^{-\frac{1}{2} z \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \sqrt{\epsilon_0} f^{(0,0,1)}[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]}{\sqrt{\mu_0}}$$

$$\text{In}[] := \text{term1a} = \text{D}[\text{Cross}[\mathbf{ev}, \mathbf{mv}], t]$$

$$\text{Out}[] = \{0, 0, -e^{-z \epsilon_0 \mu_0 g[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}]} z \epsilon_0^{3/2} \sqrt{\mu_0} f[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g'[t - z \sqrt{\epsilon_0} \sqrt{\mu_0}] + \dots\}$$

In[•]:=

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}.$$

In[•]:= term1 = ((-ε0)*μ0)*D[Cross[ev, mv], t]

$$\text{Out[•]} = \left\{ 0, 0, -\epsilon_0 \mu_0 \left(-e^{-z \sqrt{\epsilon_0 \mu_0} g[t-z \sqrt{\epsilon_0 \mu_0}]} z \epsilon_0^{3/2} \sqrt{\mu_0} f[t-z \sqrt{\epsilon_0 \mu_0}, x, y]^2 g'[t-z \sqrt{\epsilon_0 \mu_0}] \right) \right\}$$

In[•]:=

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}).$$

In[•]:= term2 = ε0*ev*Div[ev]

$$\text{Out[•]} = \left\{ e^{-z \sqrt{\epsilon_0 \mu_0} g[t-z \sqrt{\epsilon_0 \mu_0}]} \epsilon_0 f[t-z \sqrt{\epsilon_0 \mu_0}, x, y] f^{(0,1,0)}[t-z \sqrt{\epsilon_0 \mu_0}, x, y], 0, 0 \right\}$$

In[•]:=

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}).$$

In[•]:= term3 = (-ε0)*Cross[ev, Curl[ev]]

$$\text{Out[•]} = \left\{ 0, -e^{-z \sqrt{\epsilon_0 \mu_0} g[t-z \sqrt{\epsilon_0 \mu_0}]} \epsilon_0 f[t-z \sqrt{\epsilon_0 \mu_0}, x, y] f^{(0,0,1)}[t-z \sqrt{\epsilon_0 \mu_0}, x, y], \right. \\ \left. -\epsilon_0 \left(-\frac{1}{2} e^{-z \sqrt{\epsilon_0 \mu_0} g[t-z \sqrt{\epsilon_0 \mu_0}]} \epsilon_0 \mu_0 f[t-z \sqrt{\epsilon_0 \mu_0}, x, y]^2 g[t-z \sqrt{\epsilon_0 \mu_0}] + \frac{1}{2} e^{-z \sqrt{\epsilon_0 \mu_0} g[t-z \sqrt{\epsilon_0 \mu_0}]} \sqrt{\epsilon_0 \mu_0} f[t-z \sqrt{\epsilon_0 \mu_0}, x, y] f^{(1,0,0)}[t-z \sqrt{\epsilon_0 \mu_0}, x, y] \right) \right\}$$

In[•]:=

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}).$$

In[•]:= term4 = μ0*mv*Div[mv]

$$\text{Out[•]} = \left\{ 0, e^{-z \sqrt{\epsilon_0 \mu_0} g[t-z \sqrt{\epsilon_0 \mu_0}]} \epsilon_0 f[t-z \sqrt{\epsilon_0 \mu_0}, x, y] f^{(0,0,1)}[t-z \sqrt{\epsilon_0 \mu_0}, x, y], 0 \right\}$$

In[•]:=

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}).$$

`In[]:= term5 = (-μ0)*Cross[mv, Curl[mv]]`

`Out[]:=`
$$\left\{ -e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0 f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y] f^{(0,1,0)}[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y], 0, \right.$$

$$-\mu_0 \left(-\frac{1}{2} e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0^2 f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] + \frac{1}{2} e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0^3 f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y] f^{(1,0,0)}[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y] \right) \frac{1}{\sqrt{\mu_0}}$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) g$$

`In[]:= term6 = -\left(\frac{\epsilon_0^2 \mu_0}{2} \text{Dot}[ev, ev] + \frac{\epsilon_0 \mu_0^2}{2} \text{Dot}[mv, mv] \right) gv`

`Out[]:=`
$$\left\{ 0, 0, -e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0^2 \mu_0 f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right\}$$

`In[]:= vergelijking = term1 + term2 + term3 + term4 + term5 + term6`

`Out[]:=`
$$\left\{ 0, 0, -e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0^2 \mu_0 f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] - \right.$$

$$\epsilon_0 \mu_0 \left(-e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} z \epsilon_0^{3/2} \sqrt{\mu_0} f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g'[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right.$$

$$\left. \mu_0 \left(-\frac{1}{2} e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0^2 f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] + \frac{1}{2} e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0^3 f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y] f^{(1,0,0)}[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y] \right) \frac{1}{\sqrt{\mu_0}} \right.$$

$$\left. \frac{1}{2} e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} z \epsilon_0^{3/2} \mu_0^{3/2} f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g'[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right\}$$

`In[]:=`

The electromagnetic force density in the x - direction equals :

`In[]:= xvergelijking = term1[[1]] + term2[[1]] + term3[[1]] + term4[[1]] + term5[[1]] + term6[[1]]`

`Out[]:= 0`

`In[]:= FullSimplify[%]`

`Out[]:= 0`

In[]:= xvergelijking1 = %

Out[]:= 0

In[]:=

The electromagnetic force density in the y - direction equals :

In[]:= yvergelijking = term1[[2]] + term2[[2]] + term3[[2]] + term4[[2]] +
term5[[2]] + term6[[2]]

Out[]:= 0

In[]:= FullSimplify[%]

Out[]:= 0

In[]:= yvergelijking1 = %

Out[]:= 0

In[]:=

The electromagnetic force density in the z - direction equals :

In[]:= zvergelijking = term1[[3]] + term2[[3]] + term3[[3]] + term4[[3]] +
term5[[3]] + term6[[3]]

Out[]:=
$$-e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0^2 \mu_0 f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] -$$

$$\epsilon_0 \mu_0 \left(-e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} z \epsilon_0^{3/2} \sqrt{\mu_0} f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g'[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] \right.$$

$$\mu_0 \left(-\frac{1}{2} e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0^2 f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] +$$

$$\frac{1}{2} e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} z \epsilon_0^{5/2} \sqrt{\mu_0} f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g'[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] - \right.$$

$$\left. \epsilon_0 \left(-\frac{1}{2} e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \epsilon_0 \mu_0 f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y]^2 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}] + \frac{1}{2} e^{-z} \right.$$

$$\left. \left. e^{-z \epsilon_0 \mu_0 g[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}]} \sqrt{\epsilon_0} \sqrt{\mu_0} f[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, y] f^{(1,0,0)}[t-z \sqrt{\epsilon_0} \sqrt{\mu_0}, x, \right.$$

In[]:= FullSimplify[%]

Out[]:= 0

In[•]:= zvergelijking1 = %

Out[•]= 0

Results force densities in resp x-direction, y-direction, z-direction

Results for the ~~electromagnetic~~ force densities in resp x-direction, y-direction, z-direction:

In[•]:= xvergelijking1

Out[•]= 0

In[•]:= yvergelijking1

Out[•]= 0

In[•]:= zvergelijking1

Out[•]= 0

According the force-density equations in the x-direction, y- equals zero in every direction. This represents the solution for e

It follows from the mathematical solution for the electromagne

$$e_v = e^{-\frac{1}{2} G_1 z \epsilon_0 \mu_0} g \left[e^{-G_1 \epsilon_0 \mu_0 (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})} \right]$$

that the **intensity increases** with the value:

$$\text{Intensity} = -\frac{1}{2} (\epsilon_0 (\text{Dot}[e_v, e_v]) + \mu_0 (\text{Dot}[m_v, m_v]))$$

$$= \frac{1}{2} \left(e^{-\frac{G_1 z \epsilon_0 \mu_0}{2}} \epsilon_0 g \left[e^{-G_1 \epsilon_0 \mu_0 (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})} \right]^2 + e^{-\frac{G_1 z \epsilon_0 \mu_0}{2}} g \left[e^{-G_1 \epsilon_0 \mu_0 (t - z \sqrt{\epsilon_0} \sqrt{\mu_0})} \right]^2 \epsilon_0 \right)$$

The Electromagnetic Energy ~~Intensity~~ is proportional to: $e^{-G_1 z \epsilon_0 \mu_0}$
distance z in the direction **opposite** to the z-direction of the gra

The frequency is proportional to the energy density ([book: Equatio](#)
energy. The speed of light remains **constant** in a gravitational f

Within a Constant Gravitational Field **G1** The observed Cosmo

$$\omega_{\text{NLGR}} = \omega_0 e^{-g z \mu_0 \varepsilon_0} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

The term $\left(\frac{\Delta \omega}{\omega} = e^{-g z \mu_0 \varepsilon_0}\right)$

in Quantum Light Theory (QLT) differs

from the second term $\frac{1}{2!} (-g z \mu_0 \varepsilon_0)^2$ in Taylors Series of the exp

the Classical Gravitational Frequency Shift:

$$\left(\frac{\Delta \omega}{\omega} = -g z \mu_0 \varepsilon_0\right) \text{ in General Relativity presented in}$$

An improved approach for testing Gravitational Redshift via
Satellite-Base three frequency links combination

Example 7

Spherical Propagation of a Beam of Light in the
radial-direction with the speed of light: $c = \frac{1}{\sqrt{\varepsilon_0 \mu_0}}$.

In[•]:= Book : [Rising of the James Webb Space Telescope and Example of a Spherical Propagation of a Beam of Light](#) , propagating in the radial – direction with the speed of light :

The input for the Electric Field Intensity $\{E(x, y, z, t) = ev\}$ and the Magnetic Field Intensity $\{H(x, y, z, t) = hv\}$ in the Field Equation for the Electromagnetic Field (Book Equation 19),

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}) = 0$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Equation (19) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} = 0$$

In[•]:= $\epsilon_0 =$

In[•]:= $\mu_0 =$

```
In[• ]:= r =.
```

```
In[• ]:=  $\theta$  =.
```

```
In[• ]:=  $\varphi$  =.
```

```
In[• ]:= t =.
```

```
In[• ]:= InverseFunctions → True
```

```
Out[• ]= InverseFunctions → True
```

```
In[• ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[• ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[• ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[• ]:= InverseFunctions → True
```

```
Out[• ]= InverseFunctions → True
```

```
In[• ]:= SetCoordinates[Spherical[r,  $\theta$ ,  $\varphi$ ]]
```

```
Out[• ]= Spherical[r,  $\theta$ ,  $\varphi$ ]
```

```
In[• ]:= {Coordinates[Spherical], CoordinateRanges[Spherical]}
```

```
Out[• ]= {{r,  $\theta$ ,  $\varphi$ }, { $0 \leq r < \infty$ ,  $0 \leq \theta \leq \pi$ ,  $-\pi < \varphi \leq \pi$ }}
```

```
In[• ]:= CoordinatesToCartesian[Coordinates[Spherical], Spherical]
```

```
Out[• ]= {r Cos[ $\varphi$ ] Sin[ $\theta$ ], r Sin[ $\theta$ ] Sin[ $\varphi$ ], r Cos[ $\theta$ ]}
```

`In[•]:=` $ev = \{0, (1/r) * f[\theta, \varphi] * g[t - (K1/r + 1) * r * \text{Sqrt}[\epsilon_0] * \text{Sqrt}[\mu_0]], 0\}$

`Out[•]:=` $\left\{0, \frac{f[\theta, \varphi] \times g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{r}, 0\right\}$

`In[•]:=` $mv = (1/\text{Sqrt}[\mu_0]) * \text{Sqrt}[\epsilon_0] * \{0, 0, (1/r) * f[\theta, \varphi] * g[t - (K1/r + 1) * r * \text{Sqrt}[\epsilon_0] * \text{Sqrt}[\mu_0]]\}$

`Out[•]:=` $\left\{0, 0, \frac{\sqrt{\epsilon_0} f[\theta, \varphi] \times g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{r \sqrt{\mu_0}}\right\}$

`In[•]:=` `Div[ev]`

`Out[•]:=` $\frac{1}{r^2} \text{Csc}[\theta] \left(\text{Cos}[\theta] f[\theta, \varphi] \times g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] + g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \right)$

`In[•]:=` `Div[mv]`

`Out[•]:=` $\frac{\sqrt{\epsilon_0} \text{Csc}[\theta] g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] f^{(0,1)}[\theta, \varphi]}{r^2 \sqrt{\mu_0}}$

`In[•]:=` `FullSimplify[%]`

`Out[•]:=` $\frac{\sqrt{\epsilon_0} \text{Csc}[\theta] g\left[t - (K1 + r) \sqrt{\epsilon_0} \sqrt{\mu_0}\right] f^{(0,1)}[\theta, \varphi]}{r^2 \sqrt{\mu_0}}$

`In[•]:=` `term1a = D[Cross[ev, mv], t]`

`Out[•]:=` $\left\{\frac{2 \sqrt{\epsilon_0} f[\theta, \varphi]^2 g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g'\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{r^2 \sqrt{\mu_0}}, 0, 0\right\}$

`In[•]:=` $\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$

— **Derivative**: $\partial \left(\mathbf{E} \times \mathbf{H} \right)$ cannot be interpreted. A partial derivative requires a subscript different

`In[]:= term1 = ((-ε0)*μ0)*D[Cross[ev, mv], t]`

$$\text{Out[]} = \left\{ -\frac{2 \epsilon_0^{3/2} \sqrt{\mu_0} f[\theta, \varphi]^2 g\left[t - \left(1 + \frac{K_1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g'\left[t - \left(1 + \frac{K_1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{r^2}, \theta, \theta \right\}$$

`In[]:= term2 = ε0 E (∇ . E)`

— **Div**: $\nabla \cdot \mathbf{E}$ cannot be interpreted. In a divergence, the del operator requires a subscript with a

`In[]:= term2 = ε0 * ev * Div[ev]`

$$\text{Out[]} = \left\{ \theta, \frac{1}{r^3} \epsilon_0 \text{Csc}[\theta] f[\theta, \varphi] \times g\left[t - \left(1 + \frac{K_1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \left(\text{Cos}[\theta] f[\theta, \varphi] \times g\left[t - \left(1 + \frac{K_1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]\right) \right\}$$

`In[]:= term3 = -ε0 E × (∇ × E)`

— **General**: $\nabla \times \mathbf{E}$ cannot be interpreted. The prefix operator ∇ cannot be combined with the b

`In[]:= term3 = (-ε0)*Cross[ev, Curl[ev]]`

$$\text{Out[]} = \left\{ \frac{\epsilon_0^{3/2} \sqrt{\mu_0} f[\theta, \varphi]^2 g\left[t - \left(1 + \frac{K_1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g'\left[t - \left(1 + \frac{K_1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{r^2}, \theta, -\frac{\epsilon_0 \text{Csc}[\theta] f[\theta, \varphi] g\left[t - \left(1 + \frac{K_1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g'\left[t - \left(1 + \frac{K_1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{r^2} \right\}$$

`In[]:= term4 = μ0 H (∇ . H)`

— **Div**: $\nabla \cdot \mathbf{H}$ cannot be interpreted. In a divergence, the del operator requires a subscript with a

`In[]:= term4 = μ0 * mv * Div[mv]`

$$\text{Out[]} = \left\{ \theta, \theta, \frac{\epsilon_0 \text{Csc}[\theta] f[\theta, \varphi] g\left[t - \left(1 + \frac{K_1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(0,1)}[\theta, \varphi]}{r^3} \right\}$$

`In[]:= term5 = -μ₀ H × (∇ × H)`

— **General**: ∇ × H cannot be interpreted. The prefix operator ∇ cannot be combined with the b

`In[]:= term5 = (-μ₀)*Cross[mv, Curl[mv]]`

$$\text{Out[]:= } \left\{ \frac{\epsilon_0^{3/2} \sqrt{\mu_0} f[\theta, \varphi]^2 g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g'\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{r^2}, \right. \\ \left. -\mu_0 \left(\frac{\epsilon_0 \cot[\theta] f[\theta, \varphi]^2 g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2}{r^3 \mu_0} + \frac{\epsilon_0 f[\theta, \varphi] g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{r^3 \mu_0} \right) \right.$$

`In[]:= vergelijking = term1 + term2 + term3 + term4 + term5`

$$\text{Out[]:= } \left\{ \theta, -\mu_0 \left(\frac{\epsilon_0 \cot[\theta] f[\theta, \varphi]^2 g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2}{r^3 \mu_0} + \frac{\epsilon_0 f[\theta, \varphi] g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{r^3} \right), \right. \\ \left. \frac{1}{r^3} \epsilon_0 \csc[\theta] f[\theta, \varphi] \times g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \left(\cos[\theta] f[\theta, \varphi] \times g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \right) \right.$$

`In[]:= rvergelijking = term1[[1]] + term2[[1]] + term3[[1]] + term4[[1]] + term5[[1]]`

`Out[]:= 0`

`In[]:= FullSimplify[%]`

`Out[]:= 0`

`In[]:= rvergelijking1 = %`

`Out[]:= 0`

`In[]:= θvergelijking = term1[[2]] + term2[[2]] + term3[[2]] + term4[[2]] + term5[[2]]`

$$\text{Out[]:= } -\mu_0 \left(\frac{\epsilon_0 \cot[\theta] f[\theta, \varphi]^2 g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2}{r^3 \mu_0} + \frac{\epsilon_0 f[\theta, \varphi] g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{r^3 \mu_0} \right) \\ + \frac{1}{r^3} \epsilon_0 \csc[\theta] f[\theta, \varphi] \times g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \left(\cos[\theta] f[\theta, \varphi] \times g\left[t - \left(1 + \frac{K1}{r}\right) r \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \right)$$


```
In[• ]:= FullSimplify[%]
```

```
Out[• ]= 0
```

```
In[• ]:=  $\theta$ vergelijking1 = %
```

```
Out[• ]= 0
```

```
In[• ]:=  $\varphi$ vergelijking = term1[3] + term2[3] + term3[3] + term4[3] +  
term5[3]
```

```
Out[• ]= 0
```

```
In[• ]:= FullSimplify[%]
```

```
Out[• ]= 0
```

```
In[• ]:=  $\varphi$ vergelijking1 = %
```

```
Out[• ]= 0
```

Results force densities in resp. r-direction, θ -direction, φ -direction

```
In[• ]:= rvergelijking1
```

```
Out[• ]= 0
```

```
In[• ]:=  $\theta$ vergelijking1
```

```
Out[• ]= 0
```

```
In[• ]:=  $\varphi$ vergelijking1
```

```
Out[• ]= 0
```

Example 8

Introduction to Black Holes

```
In[• ]:= The concept of 'GEONs' (Gravitational Electromagnetic Entities
```

John Archibald Wheeler (a close friend of Albert Einstein) created and describes Electromagnetic Fields confined by their own gravitation generated by their own electromagnetic mass (according Einstein

[Geon \(physics\)](#)

[Geons](#)

[Method of the Self – Consistent Field in General Relativity and its](#)

[Book : Rising of the James Webb Space Telescope and its Fundam](#)

The input for the Electric Field Intensity $\{E(x, y, z) = ev\}$ and the Magnetic Field in the Field Equation for the Electromagnetic Field within a constant gravitational field with acceleration 'g' in the 'r' – direction. (Book Equation 73, page 47)

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) \mathbf{g}$$

Equation (73) equals :

```
term1 + term2 + term3 + term4 + term5 + term6
```

Out[]:= 1955. Archibald been by concept Electromagnetic Entities Gravitational has in intro

```
In[ ]:=  $\epsilon_0 =.$ 
```

```
In[ ]:=  $\mu_0 =.$ 
```

```
In[ ]:= r =.
```

```
In[ ]:=  $\theta =.$ 
```

```
In[ ]:=  $\varphi =.$ 
```

```
In[ ]:= t =.
```

```
In[ ]:= Get["VectorAnalysis`"]
```

— **General**: VectorAnalysis` is now obsolete. The legacy version being loaded may conflict with

```
In[ ]:= InverseFunctions → True
```

Out[]:= InverseFunctions → True

```
In[ ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[ ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:= r = .
```

```
In[ ]:= SetCoordinates[Spherical[r,  $\theta$ ,  $\varphi$ ]]
```

```
Out[ ]:= Spherical[r,  $\theta$ ,  $\varphi$ ]
```

```
In[ ]:= {Coordinates[Spherical], CoordinateRanges[Spherical]}
```

```
Out[ ]:= {{r,  $\theta$ ,  $\varphi$ }, { $\theta \leq r < \infty$ ,  $0 \leq \theta \leq \pi$ ,  $-\pi < \varphi \leq \pi$ }}
```

```
In[ ]:= CoordinatesToCartesian[Coordinates[Spherical], Spherical]
```

```
Out[ ]:= {r Cos[ $\varphi$ ] Sin[ $\theta$ ], r Sin[ $\theta$ ] Sin[ $\varphi$ ], r Cos[ $\theta$ ]}
```

```
In[ ]:= f[r] = .
```

—  Unset: Assignment on f for f[r] not found.

```
Out[ ]:= $Failed
```

```
In[ ]:= G1 =  $6.67408 \times 10^{-11}$ 
```

```
Out[ ]:=  $6.67408 \times 10^{-11}$ 
```

```
In[ ]:= Q1 =  $1.6021765 \times 10^{-19}$ 
```

```
Out[ ]:=  $1.60218 \times 10^{-19}$ 
```

```
In[ ]:=  $\epsilon_0 = 8.85 \times 10^{-12}$ 
```

```
Out[ ]:=  $8.85 \times 10^{-12}$ 
```

```
In[ ]:=  $\mu_0 = 4 \pi 10^{-7} // N$ 
```

```
Out[ ]:=  $1.25664 \times 10^{-6}$ 
```

```
In[ ]:= G1 = .
```

```
In[ ]:= Q1 = .
```

In[•]:= $\epsilon_0 = .$

In[•]:= $\mu_0 = .$

In[•]:= $\omega = .$

In[•]:= **Book : Rising of the James Webb Space Telescope and its Funda**
To find a solution for the GEON, a 'perfect equilibrium' has to b
Pressure' which forces the GEON to expand and the 'Gravitational
To find this 'perfect equilibrium' the radial directed part 'f[r]'
azimuthal and tangetial part g[θ, φ] of the electromagnetic radi
dependent part of the radiation has to be sinusoidal.

In[•]:= $ev = \{0, f[r] \times g[\theta, \varphi] \text{Sin}[\omega t], -f[r] \times g[\theta, \varphi] \text{Cos}[\omega t]\}$

Out[•]:= $\{0, f[r] \times g[\theta, \varphi] \text{Sin}[t \omega], -\text{Cos}[t \omega] f[r] \times g[\theta, \varphi]\}$

In[•]:= $mv = (1/\text{Sqrt}[\mu_0]) \text{Sqrt}[\epsilon_0] \{0, f[r] \times g[\theta, \varphi] \text{Cos}[\omega t], f[r] \times g[\theta, \varphi] \text{Sin}[\omega t]\}$

Out[•]:= $\left\{0, \frac{\sqrt{\epsilon_0} \text{Cos}[t \omega] f[r] \times g[\theta, \varphi]}{\sqrt{\mu_0}}, \frac{\sqrt{\epsilon_0} f[r] \times g[\theta, \varphi] \text{Sin}[t \omega]}{\sqrt{\mu_0}}\right\}$

`In[•]:=` Book : Rising of the James Webb Space Telescope and its Fundamental Blindnes : Page 15, Equation
 To define the Gravitational Field for the GEON, [Newton's Shell Theorem](#) has been used.
 All the mass (which can be calculated with Einsteins : $W = m c^2$) of the confined electromagnetic

In which the gravitational acceleration 'g' of the GEON equals :

$$g = \frac{G1}{4 \pi r^2}$$

and has been oriented in the radial direction of the GEON.

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\overline{E \cdot E} \right) + \epsilon \mu^2 \left(\overline{H \cdot H} \right) \right) \overline{g}$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\overline{E \cdot E} \right) + \epsilon \mu^2 \left(\overline{H \cdot H} \right) \right) \left\{ \frac{G1}{4 \pi r^2} 0, 0 \right\}$$

in which G1 represents the total mass of the GEON.

$$\text{In[•]:= } g^v = \left\{ \frac{G1}{4 \pi r^2}, 0, 0 \right\}$$

$$\text{Out[•]:= } \left\{ \frac{G1}{4 \pi r^2}, 0, 0 \right\}$$

`In[•]:=` `ev`

$$\text{Out[•]:= } \{0, f[r] \times g[\theta, \varphi] \text{Sin}[t \omega], -\text{Cos}[t \omega] f[r] \times g[\theta, \varphi]\}$$

`In[•]:=` `Div[ev]`

$$\text{Out[•]:= } \frac{1}{r^2} \text{Csc}[\theta] \left(r \text{Cos}[\theta] f[r] \times g[\theta, \varphi] \text{Sin}[t \omega] - r \text{Cos}[t \omega] f[r] g^{(\theta,1)}[\theta, \varphi] + r f[r] S: \right)$$

`In[•]:=` `Div[mv]`

$$\text{Out[•]:= } \frac{1}{r^2} \text{Csc}[\theta] \left(\frac{r \sqrt{\epsilon \theta} \text{Cos}[\theta] \text{Cos}[t \omega] f[r] \times g[\theta, \varphi]}{\sqrt{\mu \theta}} + \frac{r \sqrt{\epsilon \theta} f[r] \text{Sin}[t \omega] g^{(\theta,1)}[\theta, \varphi]}{\sqrt{\mu \theta}} \right)$$

`In[•]:=` `FullSimplify[%]`

$$\text{Out[•]:= } \frac{\sqrt{\epsilon \theta} f[r] \left(\text{Csc}[\theta] \text{Sin}[t \omega] g^{(\theta,1)}[\theta, \varphi] + \text{Cos}[t \omega] \left(\text{Cot}[\theta] g[\theta, \varphi] + g^{(1,\theta)}[\theta, \varphi] \right) \right)}{r \sqrt{\mu \theta}}$$

`In[•]:= term1a = D[Cross[ev, mv], t]`

`Out[•]= {0, 0, 0}`

`In[•]:= term1 = ((-ε0)*μ0)*D[Cross[ev, mv], t]`

`Out[•]= {0, 0, 0}`

`In[•]:= term2 = ε0*ev*Div[ev]`

`Out[•]= {0, $\frac{1}{r^2} \epsilon_0 \text{Csc}[\theta] f[r] \times g[\theta, \varphi] \text{Sin}[t \omega] (r \text{Cos}[\theta] f[r] \times g[\theta, \varphi] \text{Sin}[t \omega] - r \text{Cos}[t \omega] \text{Csc}[\theta] f[r] \times g[\theta, \varphi])$, $-\frac{1}{r^2} \epsilon_0 \text{Cos}[t \omega] \text{Csc}[\theta] f[r] \times g[\theta, \varphi] (r \text{Cos}[\theta] f[r] \times g[\theta, \varphi] \text{Sin}[t \omega] - r \text{Cos}[t \omega] \text{Csc}[\theta] f[r] \times g[\theta, \varphi])$ }`

`In[•]:= term3 = (-ε0)*Cross[ev, Curl[ev]]`

`Out[•]= {-ε0 $\left(\frac{\text{Cos}[t \omega]^2 f[r]^2 g[\theta, \varphi]^2}{r} + \frac{f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]^2}{r} + \text{Cos}[t \omega]^2 f[r] g[\theta, \varphi] \right)$, $-\epsilon_0 \left(\frac{\text{Cos}[t \omega]^2 \text{Cot}[\theta] f[r]^2 g[\theta, \varphi]^2}{r} + \frac{\text{Cos}[t \omega] \text{Csc}[\theta] f[r]^2 g[\theta, \varphi] \text{Sin}[t \omega] g^{(\theta)}$, $-\epsilon_0 \left(\frac{\text{Cos}[t \omega] \text{Cot}[\theta] f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]}{r} + \frac{\text{Csc}[\theta] f[r]^2 g[\theta, \varphi] \text{Sin}[t \omega]^2 g^{(\theta)}$ }`

`In[•]:= term4 = μ0*mv*Div[mv]`

`Out[•]= {0, $\frac{1}{r^2} \sqrt{\epsilon_0} \sqrt{\mu_0} \text{Cos}[t \omega] \text{Csc}[\theta] f[r] \times g[\theta, \varphi] \left(\frac{r \sqrt{\epsilon_0} \text{Cos}[\theta] \text{Cos}[t \omega] f[r] \times g[\theta, \varphi]}{\sqrt{\mu_0}} \right)$, $\frac{1}{r^2} \sqrt{\epsilon_0} \sqrt{\mu_0} \text{Csc}[\theta] f[r] \times g[\theta, \varphi] \text{Sin}[t \omega] \left(\frac{r \sqrt{\epsilon_0} \text{Cos}[\theta] \text{Cos}[t \omega] f[r] \times g[\theta, \varphi]}{\sqrt{\mu_0}} \right)$ }`

`In[•]:= term5 = (-μ0)*Cross[mv, Curl[mv]]`

`Out[•]= {-μ0 $\left(\frac{\epsilon_0 \text{Cos}[t \omega]^2 f[r]^2 g[\theta, \varphi]^2}{r \mu_0} + \frac{\epsilon_0 f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]^2}{r \mu_0} + \frac{\epsilon_0 \text{Cos}[t \omega]^2 f[r]}{\mu_0} \right)$, $-\mu_0 \left(\frac{\epsilon_0 \text{Cot}[\theta] f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]^2}{r \mu_0} - \frac{\epsilon_0 \text{Cos}[t \omega] \text{Csc}[\theta] f[r]^2 g[\theta, \varphi] \text{Sin}[t \omega] g^{(\theta)}}{r \mu_0} \right)$, $-\mu_0 \left(-\frac{\epsilon_0 \text{Cos}[t \omega] \text{Cot}[\theta] f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]}{r \mu_0} + \frac{\epsilon_0 \text{Cos}[t \omega]^2 \text{Csc}[\theta] f[r]^2 g[\theta, \varphi]}{r \mu_0} \right)$ }`

In[•]:= Book : Rising of the James Webb Space Telescope and its Fundamental Blindnes : Page 15, Equation
 To define the Gravitational Field for the GEON, [Newton's Shell Theorem](#) has been used.
 All the mass (which can be calculated whith Einsteins : $W = m c^2$) of the confined electromagnetic

In which the gravitational acceleration 'g' of the GEON equals :

$$g = \frac{G1}{4 \pi r^2}$$

and has been oriented in the radial direction of the GEON.

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\overline{\mathbf{E} \cdot \mathbf{E}} \right) + \epsilon \mu^2 \left(\overline{\mathbf{H} \cdot \mathbf{H}} \right) \right) \overline{\mathbf{g}}$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\overline{\mathbf{E} \cdot \mathbf{E}} \right) + \epsilon \mu^2 \left(\overline{\mathbf{H} \cdot \mathbf{H}} \right) \right) \left\{ \frac{G1}{4 \pi r^2} 0, 0 \right\}$$

in which G1 represents the total mass of the GEON.

In[•]:= $\text{term6} = -\left(\frac{\epsilon_0 \mu_0^2}{2} \text{Dot}[\text{mv}, \text{mv}] + \frac{\epsilon_0^2 \mu_0}{2} \text{Dot}[\text{ev}, \text{ev}] \right) \text{gv}$

Out[•]= $\left\{ \frac{1}{4 \pi r^2} G1 \left(-\frac{1}{2} \epsilon_0^2 \mu_0 \left(\text{Cos}[\text{t} \omega]^2 \text{f}[\text{r}]^2 \text{g}[\theta, \varphi]^2 + \text{f}[\text{r}]^2 \text{g}[\theta, \varphi]^2 \text{Sin}[\text{t} \omega]^2 \right) - \frac{1}{2} \epsilon_0 \mu_0 \epsilon \right. \right.$

`In[•]:=` vergelijking = term1 + term2 + term3 + term4 + term5 + term6

$$\begin{aligned}
 \text{Out}[•]:= & \left\{ \frac{1}{4 \pi r^2} G1 \left(-\frac{1}{2} \epsilon \theta^2 \mu \theta \left(\text{Cos}[t \omega]^2 f[r]^2 g[\theta, \varphi]^2 + f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]^2 \right) - \frac{1}{2} \epsilon \theta \mu \epsilon \right. \right. \\
 & \epsilon \theta \left(\frac{\text{Cos}[t \omega]^2 f[r]^2 g[\theta, \varphi]^2}{r} + \frac{f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]^2}{r} + \text{Cos}[t \omega]^2 f[r] g[\theta, \varphi]^2 \right. \\
 & \mu \theta \left(\frac{\epsilon \theta \text{Cos}[t \omega]^2 f[r]^2 g[\theta, \varphi]^2}{r \mu \theta} + \frac{\epsilon \theta f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]^2}{r \mu \theta} + \frac{\epsilon \theta \text{Cos}[t \omega]^2 f[r]}{\mu \theta} \right. \\
 & \left. \left. - \epsilon \theta \left(\frac{\text{Cos}[t \omega]^2 \text{Cot}[\theta] f[r]^2 g[\theta, \varphi]^2}{r} + \frac{\text{Cos}[t \omega] \text{Csc}[\theta] f[r]^2 g[\theta, \varphi] \text{Sin}[t \omega] g^{(\theta)} \right. \right. \right. \\
 & \frac{1}{r^2} \sqrt{\epsilon \theta} \sqrt{\mu \theta} \text{Cos}[t \omega] \text{Csc}[\theta] f[r] \times g[\theta, \varphi] \left(\frac{r \sqrt{\epsilon \theta} \text{Cos}[\theta] \text{Cos}[t \omega] f[r] \times g[\theta, \varphi]}{\sqrt{\mu \theta}} \right. \\
 & \frac{1}{r^2} \epsilon \theta \text{Csc}[\theta] f[r] \times g[\theta, \varphi] \text{Sin}[t \omega] \left(r \text{Cos}[\theta] f[r] \times g[\theta, \varphi] \text{Sin}[t \omega] - r \text{Cos}[t \omega] \right. \\
 & \mu \theta \left(\frac{\epsilon \theta \text{Cot}[\theta] f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]^2}{r \mu \theta} - \frac{\epsilon \theta \text{Cos}[t \omega] \text{Csc}[\theta] f[r]^2 g[\theta, \varphi] \text{Sin}[t \omega]}{r \mu \theta} \right. \\
 & \frac{1}{r^2} \sqrt{\epsilon \theta} \sqrt{\mu \theta} \text{Csc}[\theta] f[r] \times g[\theta, \varphi] \text{Sin}[t \omega] \left(\frac{r \sqrt{\epsilon \theta} \text{Cos}[\theta] \text{Cos}[t \omega] f[r] \times g[\theta, \varphi]}{\sqrt{\mu \theta}} \right. \\
 & \left. \left. \left. \epsilon \theta \left(\frac{\text{Cos}[t \omega] \text{Cot}[\theta] f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]}{r} + \frac{\text{Csc}[\theta] f[r]^2 g[\theta, \varphi] \text{Sin}[t \omega]^2 g^{(\theta)}}{r} \right. \right. \right. \\
 & \mu \theta \left(-\frac{\epsilon \theta \text{Cos}[t \omega] \text{Cot}[\theta] f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]}{r \mu \theta} + \frac{\epsilon \theta \text{Cos}[t \omega]^2 \text{Csc}[\theta] f[r]^2 g[\theta, \varphi]}{r \mu \theta} \right. \\
 & \left. \left. \left. \frac{1}{r^2} \epsilon \theta \text{Cos}[t \omega] \text{Csc}[\theta] f[r] \times g[\theta, \varphi] \left(r \text{Cos}[\theta] f[r] \times g[\theta, \varphi] \text{Sin}[t \omega] - r \text{Cos}[t \omega] \right. \right. \right.
 \end{aligned}$$

`In[•]:=` rvergelijking = term1[1] + term2[1] + term3[1] + term4[1] + term5[1] + term6[1]

$$\begin{aligned}
 \text{Out}[•]:= & \frac{1}{4 \pi r^2} G1 \left(-\frac{1}{2} \epsilon \theta^2 \mu \theta \left(\text{Cos}[t \omega]^2 f[r]^2 g[\theta, \varphi]^2 + f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]^2 \right) - \frac{1}{2} \epsilon \theta \mu \theta^2 \right. \\
 & \epsilon \theta \left(\frac{\text{Cos}[t \omega]^2 f[r]^2 g[\theta, \varphi]^2}{r} + \frac{f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]^2}{r} + \text{Cos}[t \omega]^2 f[r] g[\theta, \varphi]^2 \right. \\
 & \left. \left. \mu \theta \left(\frac{\epsilon \theta \text{Cos}[t \omega]^2 f[r]^2 g[\theta, \varphi]^2}{r \mu \theta} + \frac{\epsilon \theta f[r]^2 g[\theta, \varphi]^2 \text{Sin}[t \omega]^2}{r \mu \theta} + \frac{\epsilon \theta \text{Cos}[t \omega]^2 f[r]}{\mu \theta} \right. \right.
 \end{aligned}$$

`In[•]:=` FullSimplify[%]

$$\text{Out}[•]:= -\frac{\epsilon \theta f[r] g[\theta, \varphi]^2 \left((8 \pi r + G1 \epsilon \theta \mu \theta) f[r] + 8 \pi r^2 f'[r] \right)}{4 \pi r^2}$$

In[•]:= rvergelijking1 = %

$$\text{Out[•]} = -\frac{\epsilon_0 f[r] g[\theta, \varphi]^2 \left((8 \pi r + G_1 \epsilon_0 \mu_0) f[r] + 8 \pi r^2 f'[r] \right)}{4 \pi r^2}$$

In[•]:= θ vergelijking = term1[2] + term2[2] + term3[2] + term4[2] + term5[2] + term6[2]

$$\begin{aligned} \text{Out[•]} = & -\epsilon_0 \left(\frac{\cos[t \omega]^2 \cot[\theta] f[r]^2 g[\theta, \varphi]^2}{r} + \frac{\cos[t \omega] \csc[\theta] f[r]^2 g[\theta, \varphi] \sin[t \omega] g^{(0,1)}}{r} \right. \\ & \frac{1}{r^2} \sqrt{\epsilon_0} \sqrt{\mu_0} \cos[t \omega] \csc[\theta] f[r] \times g[\theta, \varphi] \left(\frac{r \sqrt{\epsilon_0} \cos[\theta] \cos[t \omega] f[r] \times g[\theta, \varphi]}{\sqrt{\mu_0}} \right. \\ & \left. \frac{1}{r^2} \epsilon_0 \csc[\theta] f[r] \times g[\theta, \varphi] \sin[t \omega] \left(r \cos[\theta] f[r] \times g[\theta, \varphi] \sin[t \omega] - r \cos[t \omega] \right. \right. \\ & \left. \left. \mu_0 \left(\frac{\epsilon_0 \cot[\theta] f[r]^2 g[\theta, \varphi]^2 \sin[t \omega]^2}{r \mu_0} - \frac{\epsilon_0 \cos[t \omega] \csc[\theta] f[r]^2 g[\theta, \varphi] \sin[t \omega]}{r \mu_0} \right) \right) \right. \end{aligned}$$

In[•]:= FullSimplify[%]

$$\text{Out[•]} = 0$$

In[•]:= θ vergelijking1 = %

$$\text{Out[•]} = 0$$

In[•]:= φ vergelijking = term1[3] + term2[3] + term3[3] + term4[3] + term5[3] + term6[3]

$$\begin{aligned} \text{Out[•]} = & \frac{1}{r^2} \sqrt{\epsilon_0} \sqrt{\mu_0} \csc[\theta] f[r] \times g[\theta, \varphi] \sin[t \omega] \left(\frac{r \sqrt{\epsilon_0} \cos[\theta] \cos[t \omega] f[r] \times g[\theta, \varphi]}{\sqrt{\mu_0}} + \right. \\ & \epsilon_0 \left(\frac{\cos[t \omega] \cot[\theta] f[r]^2 g[\theta, \varphi]^2 \sin[t \omega]}{r} + \frac{\csc[\theta] f[r]^2 g[\theta, \varphi] \sin[t \omega]^2 g^{(0,1)}}{r} \right. \\ & \left. \mu_0 \left(-\frac{\epsilon_0 \cos[t \omega] \cot[\theta] f[r]^2 g[\theta, \varphi]^2 \sin[t \omega]}{r \mu_0} + \frac{\epsilon_0 \cos[t \omega]^2 \csc[\theta] f[r]^2 g[\theta, \varphi]}{r \mu_0} \right) \right. \\ & \left. \frac{1}{r^2} \epsilon_0 \cos[t \omega] \csc[\theta] f[r] \times g[\theta, \varphi] \left(r \cos[\theta] f[r] \times g[\theta, \varphi] \sin[t \omega] - r \cos[t \omega] \right) \right) \end{aligned}$$

In[•]:= FullSimplify[%]

$$\text{Out[•]} = 0$$

In[]:= φ vergelijking1 = %

Out[]:= 0

Results force densities in resp r-direction, θ -direction, φ -direction

In[]:= rvergelijking1

Out[]:=
$$-\frac{\epsilon_0 f[r] g[\theta, \varphi]^2 \left((8 \pi r + G_1 \epsilon_0 \mu_0) f[r] + 8 \pi r^2 f'[r] \right)}{4 \pi r^2}$$

In[]:= θ vergelijking1

Out[]:= 0

In[]:= φ vergelijking1

Out[]:= 0

Example 5

Gravitational-Electromagnetic confinement for GEONs.

In[]:= **Book** : [Rising of the James Webb Space Telescope and its Fundamentals](#)

To establish a 'Perfect Equilibrium' between the radiation pressure and the gravitational confining force density, the 'rvergelijking1' in

$$(8 \pi r + G_1 \epsilon_0 \mu_0) f[r] + 8 \pi r^2 f'[r] = 0$$

In[]:= f[r] = .

— **Unset**: Assignment on f for f[r] not found.

Out[]:= \$Failed

In[]:= DSolve[(8 π r + G1 ϵ_0 μ_0) f[r] + 8 π r² f'[r] == 0, f[r], r]

Out[]:=
$$\left\{ \left\{ f[r] \rightarrow e^{-\frac{G_1 \epsilon_0 \mu_0}{r} + 8 \pi \log[r]} c_1 \right\} \right\}$$

In[•]:= The solution for Equation (73) in the radial direction equals :

$$f[r] = K1 e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}}$$

in which K1 an arbitrary value.

— **Set**: Tag Times in 73 direction Equation for in radial solution the The (equals : f[r]) is Protecte

Out[•]= $e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1$

In[]:= Book : Rising of the James Webb Space Telescope and its Fundam

The input for the Electric Field Intensity $\{E(x, y, z) = ev\}$ and the Mag
in the Field Equation for the Electromagnetic Field within a constant gra
with acceleration 'g' in the 'r' - direction. (Book Equation 73, page 47)

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) \mathbf{g}$$

Equation (73) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} + \text{term6}$$

In[]:= $\epsilon_0 =$

In[]:= $\mu_0 =$

```
In[ ]:= r =.
```

```
In[ ]:=  $\theta$  =.
```

```
In[ ]:=  $\varphi$  =.
```

```
In[ ]:= t =.
```

```
In[ ]:= InverseFunctions → True
```

```
Out[ ]= InverseFunctions → True
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```


```
In[ ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[ ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:= InverseFunctions → True
```

```
Out[ ]= InverseFunctions → True
```

```
In[ ]:= Get["VectorAnalysis`"]
```

—  **General**: VectorAnalysis` is now obsolete. The legacy version being loaded may conflict wit

```
In[ ]:= r = .
```

```
In[ ]:= SetCoordinates[Spherical[r,  $\theta$ ,  $\varphi$ ]]
```

```
Out[ ]= Spherical[r,  $\theta$ ,  $\varphi$ ]
```

```
In[ ]:= {Coordinates[Spherical], CoordinateRanges[Spherical]}
```

```
Out[ ]= {{r,  $\theta$ ,  $\varphi$ }, { $\theta \leq r < \infty$ ,  $\theta \leq \theta \leq \pi$ ,  $-\pi < \varphi \leq \pi$ }}
```

`In[]:= CoordinatesToCartesian[Coordinates[Spherical], Spherical]`

`Out[]:= {r Cos[φ] Sin[θ], r Sin[θ] Sin[φ], r Cos[θ]}`

`In[]:= f[r] = .`

— **Unset**: Assignment on f for f[r] not found.

`Out[]:= $Failed`

`In[]:= n = .`

`In[]:= ε0 = .`

`In[]:= μ0 = .`

`In[]:= Q1 = .`

`In[]:= G1 = 6.67408 × 10-11`

`Out[]:= 6.67408 × 10-11`

`In[]:= Q1 = 1.6021765 × 10-19`

`Out[]:= 1.60218 × 10-19`

`In[]:= ε0 = 8.85 × 10-12`

`Out[]:= 8.85 × 10-12`

`In[]:= μ0 = 4 π 10-7 // N`

`Out[]:= 1.25664 × 10-6`

`In[]:= G1 = .`

In[•]:= Q1 = .

In[•]:= $\epsilon_0 = .$

In[•]:= $\mu_0 = .$

In[•]:= $f[r] = K1 e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}}$

Out[•]:= $e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1$

In[•]:= $ev = \{0, f[r] \text{Sin}[\omega t], -f[r] \text{Cos}[t \omega]\}$

Out[•]:= $\left\{0, e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \text{Sin}[t \omega], -e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \text{Cos}[t \omega]\right\}$

In[•]:= $mv = (1/\text{Sqrt}[\mu_0]) \text{Sqrt}[\epsilon_0] \{0, f[r] \text{Cos}[t \omega], f[r] \text{Sin}[t \omega]\}$

Out[•]:= $\left\{0, \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \sqrt{\epsilon_0} \text{Cos}[t \omega]}{\sqrt{\mu_0}}, \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \sqrt{\epsilon_0} \text{Sin}[t \omega]}{\sqrt{\mu_0}}\right\}$

In[•]:= $gv = \left\{\frac{G1}{4 \pi r^2}, 0, 0\right\}$

Out[•]:= $\left\{\frac{G1}{4 \pi r^2}, 0, 0\right\}$

In[•]:= ev

Out[•]:= $\left\{0, e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \text{Sin}[t \omega], -e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \text{Cos}[t \omega]\right\}$

In[•]:= $\text{Div}[ev]$

Out[•]:= $\frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \text{Cot}[\theta] \text{Sin}[t \omega]}{r}$

In[•]:= Div[mv]

$$\text{Out[•]} = \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \sqrt{\epsilon_0} \text{Cos}[t \omega] \text{Cot}[\theta]}{r \sqrt{\mu_0}}$$

In[•]:= FullSimplify[%]

$$\text{Out[•]} = \frac{e^{\frac{G1 \epsilon_0 \mu_0}{8 \pi r}} K1 \sqrt{\epsilon_0} \text{Cos}[t \omega] \text{Cot}[\theta]}{r^2 \sqrt{\mu_0}}$$

In[•]:= term1a = D[Cross[ev, mv], t]

$$\text{Out[•]} = \{0, 0, 0\}$$

In[•]:= term1 = ((-ε0)*μ0)*D[Cross[ev, mv], t]

$$\text{Out[•]} = \{0, 0, 0\}$$

In[•]:= term2 = ε0*ev*Div[ev]

$$\text{Out[•]} = \left\{ 0, \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} K1^2 \epsilon_0 \text{Cot}[\theta] \text{Sin}[t \omega]^2}{r}, -\frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} K1^2 \epsilon_0 \text{Cos}[t \omega] \text{Cot}[\theta]}{r} \right\}$$

In[•]:= term3 = (-ε0)*Cross[ev, Curl[ev]]

$$\text{Out[•]} = \left\{ -\epsilon_0 \left(-\frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} G1 K1^2 \epsilon_0 \mu_0 \text{Cos}[t \omega]^2}{8 \pi r^2} - \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} G1 K1^2 \epsilon_0 \mu_0 \text{Sin}[t \omega]^2}{8 \pi r^2} \right) \right\}$$

In[•]:= term4 = μ0*mv*Div[mv]

$$\text{Out[•]} = \left\{ 0, \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} K1^2 \epsilon_0 \text{Cos}[t \omega]^2 \text{Cot}[\theta]}{r}, \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} K1^2 \epsilon_0 \text{Cos}[t \omega] \text{Cot}[\theta]}{r} \right\}$$

In[•]:= term5 = (-μ0)*Cross[mv, Curl[mv]]

$$\text{Out}[•] = \left\{ -\mu\theta \left(-\frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \cos[t\omega]^2}{8\pi r^4} - \frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \sin[t\omega]^2}{8\pi r^4} \right), -\frac{e^{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \log[r]}}{4\pi} \right\}$$

In[•]:= term6 = -\left(\frac{\epsilon\theta \mu\theta^2}{2} \text{Dot}[mv, mv] + \frac{\epsilon\theta^2 \mu\theta}{2} \text{Dot}[ev, ev]\right) gv

$$\text{Out}[•] = \left\{ \frac{1}{4\pi r^2} G1 \left(-\frac{1}{2} \epsilon\theta^2 \mu\theta \left(e^{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \log[r]} K1^2 \cos[t\omega]^2 + e^{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \log[r]} K1^2 \sin[t\omega]^2 \right) \right. \right.$$

In[•]:= vergelijking = term1 + term2 + term3 + term4 + term5 + term6

$$\text{Out}[•] = \left\{ -\mu\theta \left(-\frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \cos[t\omega]^2}{8\pi r^4} - \frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \sin[t\omega]^2}{8\pi r^4} \right) - \epsilon\theta \left(-\frac{e^{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \log[r]}}{4\pi} \right. \right.$$

$$\left. \left. \frac{1}{4\pi r^2} G1 \left(-\frac{1}{2} \epsilon\theta^2 \mu\theta \left(e^{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \log[r]} K1^2 \cos[t\omega]^2 + e^{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \log[r]} K1^2 \sin[t\omega]^2 \right) \right) \right\}$$

In[•]:= rvergelijking = term1[[1]] + term2[[1]] + term3[[1]] + term4[[1]] + term5[[1]] + term6[[1]]

$$\text{Out}[•] = -\mu\theta \left(-\frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \cos[t\omega]^2}{8\pi r^4} - \frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \sin[t\omega]^2}{8\pi r^4} \right) - \epsilon\theta \left(-\frac{e^{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \log[r]}}{4\pi} \right.$$

$$\left. \left. \frac{1}{4\pi r^2} G1 \left(-\frac{1}{2} \epsilon\theta^2 \mu\theta \left(e^{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \log[r]} K1^2 \cos[t\omega]^2 + e^{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \log[r]} K1^2 \sin[t\omega]^2 \right) \right) \right\}$$

In[•]:= FullSimplify[%]

Out[•] = 0

In[•]:= rvergelijking1 = %

Out[•] = 0

```
In[• ]:=  $\theta$ vergelijking = term1[2] + term2[2] + term3[2] + term4[2] +
term5[2] + term6[2]
```

Out[•]= 0

```
In[• ]:= FullSimplify[%]
```

Out[•]= 0

```
In[• ]:=  $\theta$ vergelijking1 = %
```

Out[•]= 0

```
In[• ]:=  $\varphi$ vergelijking = term1[3] + term2[3] + term3[3] + term4[3] +
term5[3] + term6[3]
```

Out[•]= 0

```
In[• ]:= FullSimplify[%]
```

Out[•]= 0

```
In[• ]:=  $\varphi$ vergelijking1 = %
```

Out[•]= 0

Results force densities in resp r-direction, θ -direction, φ -direction

```
In[• ]:= rvergelijking1
```

Out[•]= 0

```
In[• ]:=  $\theta$ vergelijking1
```

Out[•]= 0

```
In[• ]:=  $\varphi$ vergelijking1
```

Out[•]= 0

To establish a **‘Perfect Equilibrium’** between the radiation pressure,

and the gravitational confining force density in the radial r -direction electromagnetic force density equals zero in every direction. This rep

This result represents Newton's ideas about a **Universal Harmony**.

Example 6

Graphical Presentation of a GEON.

In[•]:= The concept of ' GEONs ' (Gravitational Electromagnetic Entities

Book : [Rising of the James Webb Space Telescope and its Fundam](#)

The input for the Electric Field Intensity $\{E(x, y, z) = ev\}$ and the Mag
in the Field Equation for the Electromagnetic Field within a constant gra
with acceleration ' g ' in the ' r ' – direction. (Book Equation 73, page 47

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

$$\text{term6} = -\frac{1}{2} \left(\epsilon^2 \mu \left(\mathbf{E} \cdot \mathbf{E} \right) + \epsilon \mu^2 \left(\mathbf{H} \cdot \mathbf{H} \right) \right) \mathbf{g}$$

Equation (73) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} + \text{term6}$$

Out[•]:= 1955. Archibald been by concept Electromagnetic Entities Gravitational has in into

In[•]:= $\epsilon_0 =$.

```
In[ ]:=  $\mu_0 = .$ 
```

```
In[ ]:=  $r = .$ 
```

```
In[ ]:=  $\theta = .$ 
```

```
In[ ]:=  $\varphi = .$ 
```

```
In[ ]:=  $t = .$ 
```

```
In[ ]:= InverseFunctions  $\rightarrow$  True
```

```
Out[ ]:= InverseFunctions  $\rightarrow$  True
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```


```
In[ ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[ ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:= InverseFunctions  $\rightarrow$  True
```

```
Out[ ]:= InverseFunctions  $\rightarrow$  True
```

```
In[ ]:= Get["VectorAnalysis`"]
```

—  **General**: VectorAnalysis` is now obsolete. The legacy version being loaded may conflict wit

```
In[ ]:=  $r = .$ 
```

```
In[ ]:= SetCoordinates[Spherical[r,  $\theta$ ,  $\varphi$ ]]
```

```
Out[ ]:= Spherical[r,  $\theta$ ,  $\varphi$ ]
```

In[•]:= `{Coordinates[Spherical], CoordinateRanges[Spherical]}`

Out[•]= `{{r, θ , φ }, { $\theta \leq r < \infty$, $0 \leq \theta \leq \pi$, $-\pi < \varphi \leq \pi$ }}`

In[•]:= `CoordinatesToCartesian[Coordinates[Spherical], Spherical]`

Out[•]= `{r Cos [φ] Sin [θ], r Sin [θ] Sin [φ], r Cos [θ] }`

In[•]:= `f[r] = .`

In[•]:= `n = .`

In[•]:= `ϵ_0 = .`

In[•]:= `μ_0 = .`

In[•]:= `Q1 = .`

In[•]:= `G1 = 6.67408×10^{-11}`

Out[•]= `6.67408×10^{-11}`

In[•]:= `Q1 = $1.6021765 \times 10^{-19}$`

Out[•]= `1.60218×10^{-19}`

In[•]:= `ϵ_0 = 8.85×10^{-12}`

Out[•]= `8.85×10^{-12}`

In[•]:= `μ_0 = $4 \pi 10^{-7}$ // N`

Out[•]= `1.25664×10^{-6}`

In[•]:= `G1 = .`

In[•]:= Q1 = .

In[•]:= $\epsilon_0 = .$

In[•]:= $\mu_0 = .$

In[•]:= $f[r] = K1 e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}}$

Out[•]:= $e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1$

In[•]:= $ev = \{0, f[r] \text{Sin}[\omega t], -f[r] \text{Cos}[t \omega]\}$

Out[•]:= $\{0, e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \text{Sin}[t \omega], -e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \text{Cos}[t \omega]\}$

In[•]:= $mv = (1/\text{Sqrt}[\mu_0]) \text{Sqrt}[\epsilon_0] \{0, f[r] \text{Cos}[t \omega], f[r] \text{Sin}[t \omega]\}$

Out[•]:= $\{0, \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \sqrt{\epsilon_0} \text{Cos}[t \omega]}{\sqrt{\mu_0}}, \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \sqrt{\epsilon_0} \text{Sin}[t \omega]}{\sqrt{\mu_0}}\}$

In[•]:= $gv = \left\{\frac{G1}{4 \pi r^2}, 0, 0\right\}$

Out[•]:= $\left\{\frac{G1}{4 \pi r^2}, 0, 0\right\}$

In[•]:= ev

Out[•]:= $\{0, e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \text{Sin}[t \omega], -e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \text{Cos}[t \omega]\}$

In[•]:= $\text{Div}[ev]$

Out[•]:= $\frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \text{Cot}[\theta] \text{Sin}[t \omega]}{r}$

In[•]:= Div[mv]

$$\text{Out[•]} = \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1 \sqrt{\epsilon_0} \text{Cos}[t \omega] \text{Cot}[\theta]}{r \sqrt{\mu_0}}$$

In[•]:= FullSimplify[%]

$$\text{Out[•]} = \frac{e^{\frac{G1 \epsilon_0 \mu_0}{8 \pi r}} K1 \sqrt{\epsilon_0} \text{Cos}[t \omega] \text{Cot}[\theta]}{r^2 \sqrt{\mu_0}}$$

In[•]:= term1a = D[Cross[ev, mv], t]

$$\text{Out[•]} = \{0, 0, 0\}$$

In[•]:= term1 = ((-ε0)*μ0)*D[Cross[ev, mv], t]

$$\text{Out[•]} = \{0, 0, 0\}$$

In[•]:= term2 = ε0*ev*Div[ev]

$$\text{Out[•]} = \left\{ 0, \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} K1^2 \epsilon_0 \text{Cot}[\theta] \text{Sin}[t \omega]^2}{r}, -\frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} K1^2 \epsilon_0 \text{Cos}[t \omega] \text{Cot}[\theta]}{r} \right\}$$

In[•]:= term3 = (-ε0)*Cross[ev, Curl[ev]]

$$\text{Out[•]} = \left\{ -\epsilon_0 \left(-\frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} G1 K1^2 \epsilon_0 \mu_0 \text{Cos}[t \omega]^2}{8 \pi r^2} - \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} G1 K1^2 \epsilon_0 \mu_0 \text{Sin}[t \omega]^2}{8 \pi r^2} \right) \right\}$$

In[•]:= term4 = μ0*mv*Div[mv]

$$\text{Out[•]} = \left\{ 0, \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} K1^2 \epsilon_0 \text{Cos}[t \omega]^2 \text{Cot}[\theta]}{r}, \frac{e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{4 \pi}} K1^2 \epsilon_0 \text{Cos}[t \omega] \text{Cot}[\theta]}{r} \right\}$$

In[•]:= term5 = (-μ0)*Cross[mv, Curl[mv]]

$$\text{Out}[•] = \left\{ -\mu\theta \left(-\frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \text{Cos}[t \omega]^2}{8\pi r^4} - \frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \text{Sin}[t \omega]^2}{8\pi r^4} \right), -\frac{e^{-\frac{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \text{Log}[r]}{4\pi}}}{4\pi} \right\}$$

In[•]:= term6 = -\left(\frac{\epsilon\theta \mu\theta^2}{2} \text{Dot}[mv, mv] + \frac{\epsilon\theta^2 \mu\theta}{2} \text{Dot}[ev, ev]\right) gv

$$\text{Out}[•] = \left\{ \frac{1}{4\pi r^2} G1 \left(-\frac{1}{2} \epsilon\theta^2 \mu\theta \left(e^{-\frac{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \text{Log}[r]}{4\pi}} K1^2 \text{Cos}[t \omega]^2 + e^{-\frac{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \text{Log}[r]}{4\pi}} K1^2 \text{Sin}[t \omega]^2 \right) \right. \right.$$

In[•]:= vergelijking = term1 + term2 + term3 + term4 + term5 + term6

$$\text{Out}[•] = \left\{ -\mu\theta \left(-\frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \text{Cos}[t \omega]^2}{8\pi r^4} - \frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \text{Sin}[t \omega]^2}{8\pi r^4} \right) - \epsilon\theta \left(-\frac{e^{-\frac{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \text{Log}[r]}{4\pi}}}{4\pi} \right. \right.$$

$$\left. \left. \frac{1}{4\pi r^2} G1 \left(-\frac{1}{2} \epsilon\theta^2 \mu\theta \left(e^{-\frac{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \text{Log}[r]}{4\pi}} K1^2 \text{Cos}[t \omega]^2 + e^{-\frac{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \text{Log}[r]}{4\pi}} K1^2 \text{Sin}[t \omega]^2 \right) \right) \right. \right.$$

In[•]:= rvergelijking = term1[[1]] + term2[[1]] + term3[[1]] + term4[[1]] + term5[[1]] + term6[[1]]

$$\text{Out}[•] = -\mu\theta \left(-\frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \text{Cos}[t \omega]^2}{8\pi r^4} - \frac{e^{\frac{G1 \epsilon\theta \mu\theta}{4\pi r}} G1 K1^2 \epsilon\theta^2 \text{Sin}[t \omega]^2}{8\pi r^4} \right) - \epsilon\theta \left(-\frac{e^{-\frac{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \text{Log}[r]}{4\pi}}}{4\pi} \right.$$

$$\left. \left. \frac{1}{4\pi r^2} G1 \left(-\frac{1}{2} \epsilon\theta^2 \mu\theta \left(e^{-\frac{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \text{Log}[r]}{4\pi}} K1^2 \text{Cos}[t \omega]^2 + e^{-\frac{-\frac{G1 \epsilon\theta \mu\theta}{r} + 8\pi \text{Log}[r]}{4\pi}} K1^2 \text{Sin}[t \omega]^2 \right) \right) \right. \right.$$

In[•]:= FullSimplify[%]

Out[•]= 0

In[•]:= rvergelijking1 = %

Out[•]= 0

```
In[• ]:=  $\theta$ vergelijking = term1[2] + term2[2] + term3[2] + term4[2] +
term5[2] + term6[2]
```

Out[•]= 0

```
In[• ]:= FullSimplify[%]
```

Out[•]= 0

```
In[• ]:=  $\theta$ vergelijking1 = %
```

Out[•]= 0

```
In[• ]:=  $\varphi$ vergelijking = term1[3] + term2[3] + term3[3] + term4[3] +
term5[3] + term6[3]
```

Out[•]= 0

```
In[• ]:= FullSimplify[%]
```

Out[•]= 0

```
In[• ]:=  $\varphi$ vergelijking1 = %
```

Out[•]= 0

Results force densities in resp r-direction, θ -direction, φ -direction

```
In[• ]:= rvergelijking1
```

Out[•]= 0

```
In[• ]:=  $\theta$ vergelijking1
```

Out[•]= 0

```
In[• ]:=  $\varphi$ vergelijking1
```

Out[•]= 0

`In[]:=` The radial function 'f[r]' for the electromagnetic – gravitational confinement (GEON) equals : f[r] = K1
 In thebook : ' [Rising of theJamesWebb SpaceTelescope and its Fundamental Blindness](#) ', page104, Figure
 a graphic Plot has been presented for the GEON with the chosen value for K1 = 6.67408×10^{-11}

— `Set`: Tag Plus in –confinement GEON gravitational (equals : $e^{-\frac{\text{Times}[\ll 5 \gg] + \text{Times}[\ll 3 \gg]}{8 \pi} K1}$) + electro

$$\text{Out}[] = e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K1$$

`In[]:=` $\epsilon_0 = 8.85 \times 10^{-12}$

$$\text{Out}[] = 8.85 \times 10^{-12}$$

`In[]:=` $\mu_0 = 4 \pi 10^{-7}$

$$\text{Out}[] = \frac{\pi}{2500000}$$

`In[]:=` The value for the gravitational constant G1 equals

`Out[]:=` constant equals for gravitational the The value G1

`In[]:=` $G1 = 6.67408 \times 10^{-11}$

$$\text{Out}[] = 6.67408 \times 10^{-11}$$

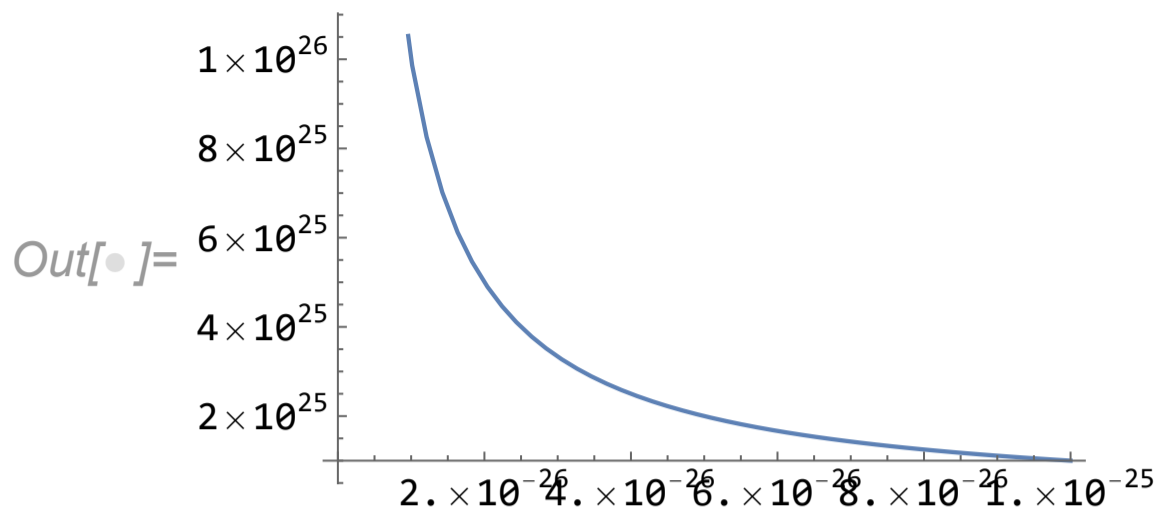
`In[]:=` $f[r] = K e^{-\frac{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}{8 \pi}}$

$$\text{Out}[] = e^{-\frac{-\frac{7.4224 \times 10^{-28}}{r} + 8 \pi \text{Log}[r]}{8 \pi}} K$$

`In[]:=` $K = 0.00001$

$$\text{Out}[] = 0.00001$$

`In[]:= Plot[$e^{-\frac{K G1 \epsilon0 \mu0}{r} + 8 \pi \text{Log}[r]}$, {r, 10-36, 10-25}`

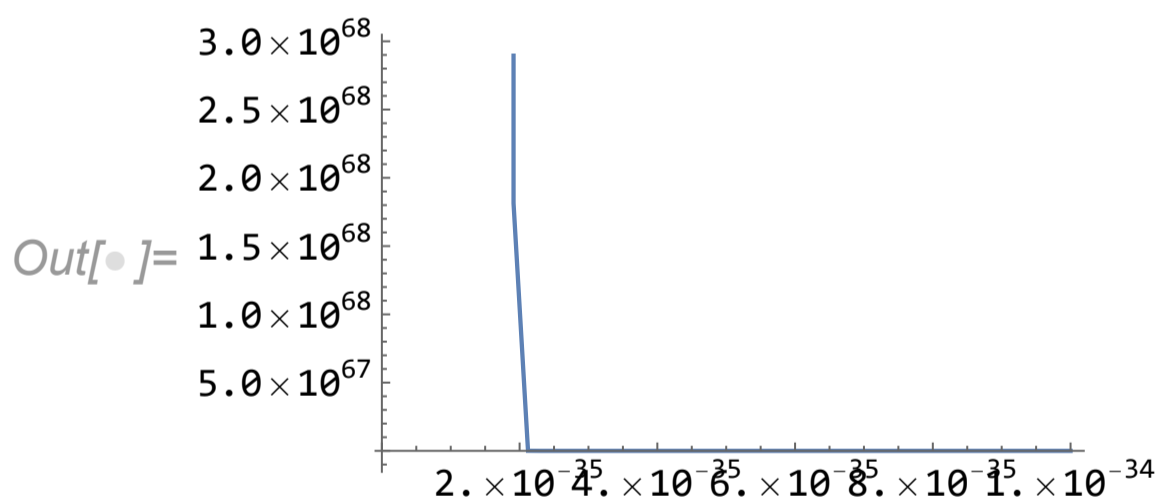


`In[]:=` In the book '[Rising of the James Webb Space Telescope](#)' Figure 5, page 105, represents the graphic Plot for the GEON with the arbitrary constant K chosen at a **five times** higher value

`In[]:= K2 = 0.00005`

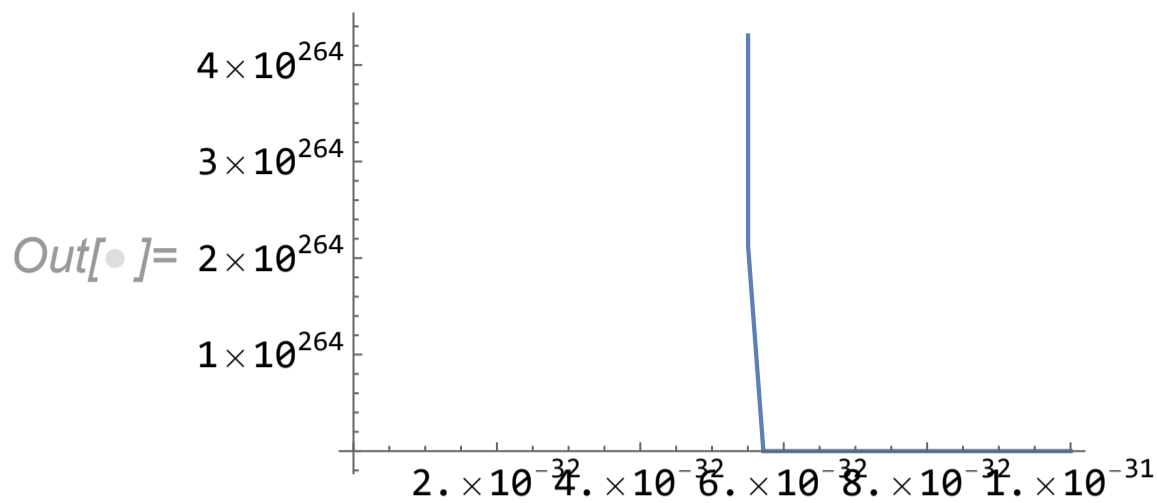
`Out[]:= 0.00005`

`In[]:= Plot[$e^{-\frac{K2 G1 \epsilon0 \mu0}{r} + 8 \pi \text{Log}[r]}$, {r, 10-36, 10-34}`



`In[]:=` Choosing for the arbitrary constant K, the value K equals 1, represents a GEON with a thousand times

In[]:= `Plot[$e^{-\frac{G1 \epsilon_0 \mu_0}{r} + 8 \pi \text{Log}[r]}$, {r, 0, 10-31}]`



In[]:= Choosing for the arbitrary constant K, the value K equals 1, represents a GEON with a thousand times intensity and the magnetic field intensity, the conclusion follows :

The stronger the electromagnetic field of the GEON,
The radius of the GEON is *inversely proportional* (Electromagnetic Mass) of the GEON.

Example 7 Universal Harmony

In[]:= Book : [Rising of the James Webb Space Telescope and its Fundamental](#)
 Isaac Newton believed like many scientists of his time in a Universal (Cosmic) Harmony
 ([Newton and the Mystery of the Major Sixth](#)) and in [Paintings](#). This

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Example of Newton's [Universal \(Cosmic\) Harmony](#) within an arbitrary region of space with an arbitrary 'Electric and Magnetic Field Intensity Division' $g[x, y, z]$

propagating in the z – direction with the speed of light $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$.

In[]:= `Needs["DifferentialEquations`NDSolveProblems`"]`

```
In[ ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[ ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:=  $\epsilon_0 = .$ 
```

```
In[ ]:=  $\mu_0 = .$ 
```


```
In[ ]:=  $x = .$ 
```

```
In[ ]:=  $y = .$ 
```

```
In[ ]:=  $z = .$ 
```

```
In[ ]:=  $t = .$ 
```

```
In[ ]:= Get["VectorAnalysis`"]
```

—  **General**: VectorAnalysis` is now obsolete. The legacy version being loaded may conflict wit

```
In[ ]:= InverseFunctions → True
```

```
Out[ ]:= InverseFunctions → True
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[ ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

```
In[ ]:= Needs["DifferentialEquations`InterpolatingFunctionAnatomy`"]
```

```
In[ ]:= SetCoordinates[Cartesian[x, y, z]]
```

```
Out[ ]:= Cartesian[x, y, z]
```

```
In[• ]:= {Coordinates[Cartesian], CoordinateRanges[Cartesian]}
```

```
Out[• ]= {{x, y, z}, {-∞ < x < ∞, -∞ < y < ∞, -∞ < z < ∞}}
```

```
In[• ]:= g[z, t]=.
```

—  **Unset**: Assignment on g for g[z, t] not found.

```
Out[• ]= $Failed
```

```
In[• ]:= f[x, y]=.
```

```
In[• ]:= f[x, y]=.
```

—  **Unset**: Assignment on f for f[x, y] not found.

```
Out[• ]= $Failed
```

```
In[• ]:= K1 = 1
```

```
Out[• ]= 1
```

```
In[• ]:= ev = {f[x, y] * g[t - (K1/z + 1) * z * Sqrt[ε0] * Sqrt[μ0]], 0, 0}
```

```
Out[• ]= {f[x, y] * g[t - (1 + 1/z) z √ε0 √μ0], 0, 0}
```

```
In[• ]:= mv = (1 / Sqrt[μ0]) * Sqrt[ε0] *
           {0, f[x, y] * g[t - (K1/z + 1) * z * Sqrt[ε0] * Sqrt[μ0]], 0}
```

```
Out[• ]= {0,  $\frac{\sqrt{\epsilon_0} f[x, y] \times g[t - (1 + \frac{1}{z}) z \sqrt{\epsilon_0} \sqrt{\mu_0}]}{\sqrt{\mu_0}}$ , 0}
```


In[•]:= Book : [Rising of the James Webb Space Telescope and](#)
 Example of a LASER – BEAM with a Gaussian Intensity distribution
 combined with an arbitrary division $g[x, y]$ in the (x, y) plane

The input for the Electric Field Intensity $\{E(x, y, z, t) = ev\}$ and the Magnetic Field Intensity $\{H(x, y, z, t) = eh\}$ in the Field Equation for the Electromagnetic Field (Book Equation 19),

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H}) = 0$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Equation (19) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} = 0$$

In[•]:= Div[ev]

$$\text{Out[•]} = g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] f^{(1,0)}[x, y]$$

In[]:= Div[mv]

$$\text{Out[]} = \frac{\sqrt{\epsilon_0} g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] f^{(0,1)}[x, y]}{\sqrt{\mu_0}}$$

In[]:= FullSimplify[%]

$$\text{Out[]} = \frac{\sqrt{\epsilon_0} g\left[t - (1 + z) \sqrt{\epsilon_0} \sqrt{\mu_0}\right] f^{(0,1)}[x, y]}{\sqrt{\mu_0}}$$

In[]:= term1a = D[Cross[ev, mv], t]

$$\text{Out[]} = \left\{0, 0, \frac{2 \sqrt{\epsilon_0} f[x, y]^2 g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g'\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]}{\sqrt{\mu_0}}\right\}$$

In[]:= term1 = $-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$

— **Derivative**: $\partial \left(\mathbf{E} \times \mathbf{H} \right)$ cannot be interpreted. A partial derivative requires a subscript different

In[]:= term1 = ((-ε0)*μ0)*D[Cross[ev, mv], t]

$$\text{Out[]} = \left\{0, 0, -2 \epsilon_0^{3/2} \sqrt{\mu_0} f[x, y]^2 g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g'\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]\right\}$$

In[]:= term2 = ε0 E (∇ . E)

— **Div**: $\nabla \cdot \mathbf{E}$ cannot be interpreted. In a divergence, the del operator requires a subscript with

In[]:= term2 = ε0 * ev * Div[ev]

$$\text{Out[]} = \left\{\epsilon_0 f[x, y] g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(1,0)}[x, y], 0, 0\right\}$$

```
In[ ]:= term3 = -ε₀ E × (∇ × E)
```

— **General**: $\nabla \times \mathbf{E}$ cannot be interpreted. The prefix operator ∇ cannot be combined with the b

```
In[ ]:= term3 = (-ε₀) * Cross[ev, Curl[ev]]
```

```
Out[ ]:= {0, -ε₀ f[x, y] g[t - (1 + 1/z) z √ε₀ √μ₀]² f^(0,1)[x, y], ε₀³/² √μ₀ f[x, y]² g[t - (1
```

```
In[ ]:= term4 = μ₀ H (∇ . H)
```

— **Div**: $\nabla \cdot \mathbf{H}$ cannot be interpreted. In a divergence, the del operator requires a subscript with c

```
In[ ]:= term4 = μ₀ * mv * Div[mv]
```

```
Out[ ]:= {0, ε₀ f[x, y] g[t - (1 + 1/z) z √ε₀ √μ₀]² f^(0,1)[x, y], 0}
```

```
In[ ]:= term5 = -μ₀ H × (∇ × H)
```

— **General**: $\nabla \times \mathbf{H}$ cannot be interpreted. The prefix operator ∇ cannot be combined with the b

```
In[ ]:= term5 = (-μ₀) * Cross[mv, Curl[mv]]
```

```
Out[ ]:= {-ε₀ f[x, y] g[t - (1 + 1/z) z √ε₀ √μ₀]² f^(1,0)[x, y], 0, ε₀³/² √μ₀ f[x, y]² g[t - (1
```

In[•]:=

$$-\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t} + \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E}) - \epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E}) + \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H}) - \mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Which can be written as :

$$\text{term1} = -\frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

$$\text{term2} = \epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

$$\text{term3} = -\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

$$\text{term4} = \mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

$$\text{term5} = -\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Equation (19) equals :

$$\text{term1} + \text{term2} + \text{term3} + \text{term4} + \text{term5} = 0$$

— **Div**: $\nabla \cdot \mathbf{E}$ cannot be interpreted. In a divergence, the del operator requires a subscript with a

In[•]:= `vergelijking = term1 + term2 + term3 + term4 + term5`

Out[•]:= `{0, 0, 0}`

In[•]:= `The electromagnetic force density in the x - direction equals :`

In[•]:= `xvergelijking = term1[[1]] + term2[[1]] + term3[[1]] + term4[[1]] + term5[[1]]`

Out[•]:= `0`

```
In[• ]:= FullSimplify[%]
```

```
Out[• ]= 0
```

```
In[• ]:= xvergelijking1 = %
```

```
Out[• ]= 0
```

```
In[• ]:= The electromagnetic force density in the y - direction equals :
```

```
In[• ]:= yvergelijking = term1[[2]] + term2[[2]] + term3[[2]] + term4[[2]] +  
term5[[2]]
```

```
Out[• ]= 0
```

```
In[• ]:= FullSimplify[%]
```

```
Out[• ]= 0
```

```
In[• ]:= yvergelijking1 = %
```

```
Out[• ]= 0
```

```
In[• ]:= The electromagnetic force density in the z - direction equals :
```

```
In[• ]:= zvergelijking = term1[[3]] + term2[[3]] + term3[[3]] + term4[[3]] +  
term5[[3]]
```

```
Out[• ]= 0
```

```
In[• ]:= FullSimplify[%]
```

```
Out[• ]= 0
```

```
In[• ]:= zvergelijking1 = %
```

```
Out[• ]= 0
```

In[]:= Universal Harmony (Equilibrium)

Out[]:= Equilibrium Harmony Universal

In[]:= There are 4 fundamental forces in the universe.

1. The expanding force : Radiation Pressure
2. The confing force : Electromagnetic Interaction
3. The confining force : Gravity (second order effect of the electromagnetic confinement)
4. The inertia of Energy ($W = m c^2$, Einstein)

Together, the 4 fundamental forces realize a Universal Equilibrium. In every direction, the algebraic su

The expanding force : ' The **Electromagnetic Radiation Pressure** ' is an outward oriented electrom

$$\mathbf{f}_{emrp} = - (\nabla w)$$

in which ' w ' equals the electromagnetic energy density. The electromagnetic energy equals :

$$w = \left(\frac{\epsilon_0 \mu_0^2}{2} \text{Dot}[mv, mv] + \frac{\epsilon_0^2 \mu_0}{2} \text{Dot}[ev, ev] \right)$$

Out[]:= 4 are expanding forces fundamental in the The There universe.1. (force : Pressure R

Out[]:= 2. confing The (force : Electromagnetic Interaction)

Out[]:= 3. confining The (force : confinement effect electromagnetic Gravity of order seco

In[]:= There are 4 fundamental forces in the universe.

1. The expanding force : Radiation Pressure
2. The confing force : Electromagnetic Interaction
3. The confining force : Gravity (second order effect of the electromagnetic confinement)
4. The inertia of Energy ($W = m c^2$, Einstein)

Together, the 4 fundamental forces realize a Universal Equilibrium. In every direction, the algebraic sum of all the force densities together equals zero in any direction.

Out[]:= 4 are expanding forces fundamental in the The There universe.1. (force : Pressure R

Out[]:= 2. confing The (force : Electromagnetic Interaction)

Out[]:= 3. confining The (force : confinement effect electromagnetic Gravity of order seco

In[]:= The expanding force : ' The **Electromagnetic Radiation Pressure** ' is an outward oriented electromagneti

$$\mathbf{RaditationEMRP} = - (\nabla w)$$

in which ' w ' equals the electromagnetic energy density. The electromagnetic energy equals :

$$w = \left(\frac{\mu_0}{2} H^2 + \frac{\epsilon_0}{2} E^2 \right)$$

$$\text{In}[] := w = \left(\frac{\mu_0}{2} \text{Dot}[mv, mv] + \frac{\epsilon_0}{2} \text{Dot}[ev, ev] \right)$$

$$\text{Out}[] = \epsilon_0 f[x, y]^2 g \left[t - \left(1 + \frac{1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2$$

$$\text{In}[] := \text{RaditationEMRP} = - \left(\nabla w \right)$$

$$\text{Out}[] = -\nabla w$$

$$\text{In}[] := \text{RaditationEMRP} = - \text{Grad}[w]$$

$$\text{Out}[] = \left\{ -2 \epsilon_0 f[x, y] g \left[t - \left(1 + \frac{1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 f^{(1,0)}[x, y], -2 \epsilon_0 f[x, y] g \left[t - \left(1 + \frac{1}{z} \right) z \right. \right. \\ \left. \left. - 2 \epsilon_0 \left(- \left(\left(1 + \frac{1}{z} \right) \sqrt{\epsilon_0} \sqrt{\mu_0} \right) + \frac{\sqrt{\epsilon_0} \sqrt{\mu_0}}{z} \right) f[x, y]^2 g \left[t - \left(1 + \frac{1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right] g' \left[t - \right. \right. \right.$$

$$\text{In}[] := \text{Universal Harmony (Equilibrium) in the x - direction}$$

$$\text{Out}[] = -\text{direction} + \text{Equilibrium Harmony in the Universal x}$$

$\text{In}[] :=$ The example being used represents an electric field intensity ev in the $x -$ direction, a magnetic field into the page.

The outward oriented Electromagnetic Radiation Pressure in the $x -$ direction (Book Page 153, Equation B - 12) will be compensated by the confining 'Electromagnetic Radiation Pressure' in the $x -$ direction. The outward oriented Electromagnetic Radiation Pressure RaditationEMRP_x in the $x -$ direction is given by:

$$\text{In}[] := \text{RaditationEMRP} = - \text{Grad}[w]$$

$$\text{Out}[] = \left\{ -2 \epsilon_0 f[x, y] g \left[t - \left(1 + \frac{1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 f^{(1,0)}[x, y], -2 \epsilon_0 f[x, y] g \left[t - \left(1 + \frac{1}{z} \right) z \right. \right. \\ \left. \left. - 2 \epsilon_0 \left(- \left(\left(1 + \frac{1}{z} \right) \sqrt{\epsilon_0} \sqrt{\mu_0} \right) + \frac{\sqrt{\epsilon_0} \sqrt{\mu_0}}{z} \right) f[x, y]^2 g \left[t - \left(1 + \frac{1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right] g' \left[t - \right. \right. \right.$$

$$\text{In}[] := \text{RaditationEMRP}_x = - \text{Grad}[w][1]$$

$$\text{Out}[] = -2 \epsilon_0 f[x, y] g \left[t - \left(1 + \frac{1}{z} \right) z \sqrt{\epsilon_0} \sqrt{\mu_0} \right]^2 f^{(1,0)}[x, y]$$

In[]:= This outward oriented force density will be compensated by the inward oriented **Electric** 'Electromagnetic Interaction Force Density' and the inward oriented **Magnetic** 'Electromagnetic Interaction Force Density' in the x – direction : (Book Page 153, Equation B – 11) equals :

The inward oriented **Electric** 'Electromagnetic Interaction Force Density' in the x – direction (Book Page 153, Equation B – 11) equals :

$$\epsilon_0 \mathbf{E} (\nabla \cdot \mathbf{E})$$

In[]:= \mathbf{e}_v

$$\text{Out[]:= } \left\{ f[x, y] \times g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right], \theta, \theta \right\}$$

In[]:= $\text{ElectricEIFDx} = \epsilon_0 \text{Div}[\mathbf{e}_v] \times \mathbf{e}_v [[1]]$

$$\text{Out[]:= } \epsilon_0 f[x, y] g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(1,\theta)}[x, y]$$

In[]:= The inward oriented **Magnetic** 'Electromagnetic Interaction Force Density' in the x – direction (Book Page 154, Equation B – 15) equals :

$$-\mu_0 \mathbf{H} \times (\nabla \times \mathbf{H})$$

Out[]:= Electromagnetic Force in Interaction inward oriented the The Density' Magnetic'

In[]:= $\text{MagneticEIFDx} = (\mu_0) * \text{Cross}[\mathbf{m}_v, \text{Curl}[\mathbf{m}_v]][[1]]$

$$\text{Out[]:= } \epsilon_0 f[x, y] g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(1,\theta)}[x, y]$$

In[]:= The total force density in the x – direction equals the **outward** oriented radiation pressure + the **inward** oriented radiation pressure

Out[]:= densities electromagnetic forces interaction inward oriented the – direction equals zero

In[]:= $\text{TotalForceDensitydirectionx} = \text{RaditationEMRPx} + \text{ElectricEIFDx} + \text{MagneticEIFDx}$

Out[]:= 0

In[]:= The total force density in the x – direction equals always zero, independent of the intensity division $f[x, y]$. This implies that for e.g. a projection of **any arbitrary** slide on a screen, there does always exist a **perfect equilibrium (Universal Harmony)** in the x – direction.

In[•]:= Universal Harmony (Equilibrium) in the y – direction

Out[•]:= –direction + Equilibrium Harmony in the Universal y

In[•]:= The example being used represents an electric field intensity e_v in the x – direction, a magnetic field into

The outward oriented Electromagnetic Radiation Pressure in the y – direction (Book Page 153, Equation B – 12) will be compensated by the confining 'Electromagnetic direction. The outward oriented Electromagnetic Radiation Pressure $R_{aditationEMRP_y}$ in the y – direction

In[•]:= $R_{aditationEMRP} = - \text{Grad}[w]$

Out[•]:= $\left\{ -2 \epsilon_0 f[x, y] g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(1,0)}[x, y], -2 \epsilon_0 f[x, y] g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(0,1)}[x, y], -2 \epsilon_0 \left(- \left(\left(1 + \frac{1}{z}\right) \sqrt{\epsilon_0} \sqrt{\mu_0}\right) + \frac{\sqrt{\epsilon_0} \sqrt{\mu_0}}{z} \right) f[x, y]^2 g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g'\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] \right\}$

In[•]:= $R_{aditationEMRP_y} = - \text{Grad}[w][[2]]$

Out[•]:= $-2 \epsilon_0 f[x, y] g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(0,1)}[x, y]$

In[•]:= This outward oriented force density will be compensated by the inward oriented Electric 'Electromagnetic Interaction Force Density' and the inward oriented Magnetic 'Electromagnetic Interaction Force Density' in the y – direction : (Book Page 154, Equation B – 15)

The inward oriented Electric 'Electromagnetic Interaction Force Density' in the y – direction (Book Page 153, Equation B – 11) equals :

$$-\epsilon_0 \mathbf{E} \times (\nabla \times \mathbf{E})$$

In[•]:= $\text{ElectricEIFD}_y = (\epsilon_0) * \text{Cross}[e_v, \text{Curl}[e_v]][[2]]$

Out[•]:= $\epsilon_0 f[x, y] g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(0,1)}[x, y]$

In[•]:= The inward oriented Magnetic 'Electromagnetic Interaction Force Density' in the y – direction (Book Page 154, Equation B – 15) equals :

$$\mu_0 \mathbf{H} (\nabla \cdot \mathbf{H})$$

Out[•]:= Electromagnetic Force in Interaction inward oriented the The Density' Magnetic'

In[]:= MagneticEIFDy = $\mu_0 \text{Div}[\text{mv}] \times \text{mv}[2]$

Out[]:= $\epsilon_0 f[x, y] g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(0,1)}[x, y]$

In[]:= The total force density in the y – direction equals the **outward** oriented radiation pressure in the y – direc

In[]:= TotalForceDensitydirectiony = RaditationEMRPy + ElectricEIFDy + MagneticEIFDy

Out[]:= 0

In[]:= The total force density in the y – direction equals always zero, independent of the intensity division f[x, y].
This implies that for e.g. a projection of **any arbitrary** slide on a screen, there does always exist a **perfect equilibrium (Universal Harmony)** in the y – direction.

In[]:= Universal Harmony (Equilibrium) in the z – direction

Out[]:= –direction + Equilibrium Harmony in the Universal z

In[]:= The example being used represents an electric field intensity ev in the x – direction, a magnetic field into

The outward oriented Electromagnetic Radiation Pressure in the z – direction (Book Page 153, Equation B – 12) **cannot** be compensated by the confining ' **Electromagnetic**

There is **no Electric Field** Component and **no Magnetic Field** Component in the z – direction. For cannot be compensated by ' **Electromagnetic** (Electric and Magnetic) **Interaction Force Densities**'. The **of Energy** ($W = m c^2$, Einstein).

The outward oriented Electromagnetic Radiation Pressure **RaditationEMRPz** in the z – direction e

In[]:= RaditationEMRP = – Grad[w]

Out[]:= $\left\{-2 \epsilon_0 f[x, y] g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(1,0)}[x, y], -2 \epsilon_0 f[x, y] g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]^2 f^{(0,1)}[x, y], -2 \epsilon_0 \left(-\left(\left(1 + \frac{1}{z}\right) \sqrt{\epsilon_0} \sqrt{\mu_0}\right) + \frac{\sqrt{\epsilon_0} \sqrt{\mu_0}}{z}\right) f[x, y]^2 g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g'\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]\right\}$

In[]:= RaditationEMRPz = – Grad[w][3]

Out[]:= $-2 \epsilon_0 \left(-\left(\left(1 + \frac{1}{z}\right) \sqrt{\epsilon_0} \sqrt{\mu_0}\right) + \frac{\sqrt{\epsilon_0} \sqrt{\mu_0}}{z}\right) f[x, y]^2 g\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right] g'\left[t - \left(1 + \frac{1}{z}\right) z \sqrt{\epsilon_0} \sqrt{\mu_0}\right]$

In[]:= FullSimplify[%]

$$\text{Out[]} = 2 \epsilon_0^{3/2} \sqrt{\mu_0} f[x, y]^2 g[t - (1 + z) \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - (1 + z) \sqrt{\epsilon_0} \sqrt{\mu_0}]$$

In[]:= This outward (forward) oriented force density in the z – direction will be compensated by the, **in the negative direction** of the z – axis oriented, 'Inertia Force Density' of Electromagnetic Energy (E

$$\text{EMInertiaz} = - \frac{1}{c^2} \frac{\partial(\mathbf{E} \times \mathbf{H})}{\partial t}$$

In[]:= $\text{EMInertiaz} = (-\epsilon_0 * \mu_0) * \text{D}[\text{Cross}[ev, mv], t][[3]]$

$$\text{Out[]} = -2 \epsilon_0^{3/2} \sqrt{\mu_0} f[x, y]^2 g[t - (1 + \frac{1}{z}) z \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - (1 + \frac{1}{z}) z \sqrt{\epsilon_0} \sqrt{\mu_0}]$$

In[]:= The total force density in the z – direction equals the **outward (forward)** oriented radiation pressure in the

In[]:= $\text{TotalForceDensitydirectionz} = \text{RaditationEMRPz} + \text{EMInertiaz}$

$$\text{Out[]} = -2 \epsilon_0 \left(- \left(\left(1 + \frac{1}{z} \right) \sqrt{\epsilon_0} \sqrt{\mu_0} \right) + \frac{\sqrt{\epsilon_0} \sqrt{\mu_0}}{z} \right) f[x, y]^2 g[t - (1 + \frac{1}{z}) z \sqrt{\epsilon_0} \sqrt{\mu_0}] g'[t - (1 + \frac{1}{z}) z \sqrt{\epsilon_0} \sqrt{\mu_0}]$$

In[]:= FullSimplify[%]

$$\text{Out[]} = 0$$

`In[]:=` The total force density in the z – direction (the direction of propagation) always equals zero, independent of the distance from the source. This implies that for e.g. a projection of **any arbitrary** slide on a screen, there does always exist a **perfect equilibrium (Universal Harmony)** in the z – direction does only exist at one single point. The speed of light 'c'.

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$

- (1). This is the Universal Law in Physics. Only at exactly the speed of light (Perfect Equilibrium) between the radiation pressure and the gravitational force.
- (2) The **direction of propagation** of a beam of light will always be in the same direction as the magnetic field direction.

According to the force-density equations in the x-direction, y-direction, and z-direction, the total force density equals zero in every direction. This **Perfect Equilibrium** does only exist at one single point. The speed of light: $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$. This represents the solution for equation (B).

Solutions in Spherical Coordinate System: Equations (10) and (11)
 $\mathbf{e}_v\{\,,\}$ symbol for Electric Field Intensity Vector, $\mathbf{m}_v\{\,,\}$ symbol for Magnetic Field Intensity Vector
 Run program by: Select All: then: (shift + return)

`In[]:=` $\epsilon_0 = .$

`In[]:=` $\mu_0 = .$

`In[]:=` $r = .$

`In[]:=` $\theta = .$

`In[]:=` $\varphi = .$

`In[]:=` $t = .$

`In[]:=` $f[r] = .$

`In[]:=` `InverseFunctions` \rightarrow `True`

`Out[]:=` `InverseFunctions` \rightarrow `True`

```
In[• ]:= Needs["DifferentialEquations`NDSolveProblems`"]
```

```
In[• ]:= Needs["DifferentialEquations`NDSolveUtilities`"]
```

—  **System`Utilities`HashTableAdd**: -- Message text not found -- (Seconds) (System`Utilities`T

—  **CloudObject**: Unable to authenticate with Wolfram Cloud server. Please try authenticating